

Revised Effective Ionic Radii and Systematic Studies of Interatomic Distances in Halides and Chalcogenides

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The effective ionic radii of Shannon & Prewitt [*Acta Cryst.* (1969), B25, 925–945] are revised to include more unusual oxidation states and coordinations. Revisions are based on new structural data, empirical bond strength–bond length relationships, and plots of (1) radii *vs* volume, (2) radii *vs* coordination number, and (3) radii *vs* oxidation state. Factors which affect radii additivity are polyhedral distortion, partial occupancy of cation sites, covalence, and metallic character. Mean $\text{Nb}^{5+}\text{--O}$ and $\text{Mo}^{6+}\text{--O}$ octahedral distances are linearly dependent on distortion. A decrease in cation occupancy increases mean $\text{Li}^+\text{--O}$, $\text{Na}^+\text{--O}$, and $\text{Ag}^+\text{--O}$ distances in a predictable manner. Covalence strongly shortens $\text{Fe}^{2+}\text{--X}$, $\text{Co}^{2+}\text{--X}$, $\text{Ni}^{2+}\text{--X}$, $\text{Mn}^{2+}\text{--X}$, $\text{Cu}^+\text{--X}$, $\text{Ag}^+\text{--X}$, and $\text{M}\text{--H}^-$ bonds as the electronegativity of X or M decreases. Smaller effects are seen for $\text{Zn}^{2+}\text{--X}$, $\text{Cd}^{2+}\text{--X}$, $\text{In}^{3+}\text{--X}$, $\text{Pb}^{2+}\text{--X}$, and $\text{Tl}^+\text{--X}$. Bonds with delocalized electrons and therefore metallic character, *e.g.* $\text{Sm}\text{--S}$, $\text{V}\text{--S}$, and $\text{Re}\text{--O}$, are significantly shorter than similar bonds with localized electrons.

Introduction

A thorough and systematic knowledge of the relative sizes of ions in halides and chalcogenides is rapidly being developed by crystal chemists as a result of (1) extensive synthesis within certain structure types, *e.g.* rocksalt, spinel, perovskite and pyrochlore; (2) preparation of new compounds with unusual oxidation states and coordination numbers; and (3) the abundance of accurate crystal structure refinements of halides, chalcogenides, and molecular inorganic compounds. A set of effective ionic radii which showed a number of systematic trends with valence, electronic spin state, and coordination was recently developed (Shannon & Prewitt, 1969, hereafter referred to as SP 69). This work has since been supplemented and improved by studies of certain groups of ions: rare earth and actinide ions (Peterson & Cunningham, 1967, 1968); tetrahedral oxyanions (Kálmán, 1971); tetravalent ions in perovskites (Fukunaga & Fujita, 1973); rare earth ions (Greis & Petzel, 1974); and tetravalent cations (Knop & Carlow, 1974).

Further, the relative sizes of certain ions or ion pairs were studied by Khan & Baur (1972): NH_4^+ ; Ribbe & Gibbs (1971): OH^- ; Wolfe & Newham (1969): $\text{Bi}^{3+}\text{--La}^{3+}$; McCarthy (1971): $\text{Eu}^{2+}\text{--Sr}^{2+}$; Silva, McDowell, Keller & Tarrant (1974): No^{2+} . These authors' results have been incorporated here into a comprehensive modification of the Shannon-Prewitt radii.

In this paper the revised list of effective ionic radii, along with the relations between radii, coordination number, and valence is presented. The factors responsible for the deviation of radii sums from additivity such as polyhedral distortion, partial occupancy of cation sites, covalence, and metallic behavior (electron delocalization) will be discussed.

Procedure

The same basic methods used in SP 69 were employed in preparing the revised list of effective ionic radii (Table 1). Some of the same assumptions were made:

(1) Additivity of both cation and anion radii to reproduce interatomic distances is valid if one considers coordination number (CN), electronic spin, covalency, repulsive forces, and polyhedral distortion.*

(2) With these limitations, radii are independent of structure type.

(3) Both cation and anion radii vary with coordination number.

(4) With a constant anion, unit-cell volumes of isostructural series are proportional (but not necessarily linearly) to the cation volumes.

Other assumptions made in SP 69 have been modified:

(1) The effects of covalency on the shortening of M–F and M–O bonds are *not* comparable.

(2) Average interatomic distances in similar polyhedra in one structure are *not* constant but vary in a predictable way with the degree of polyhedral distortion (and anion CN). Both of these modified assumptions will be discussed in detail later.

The anion radii used in SP 69 were subtracted from available average distances. Approximately 900 distances from oxide and fluoride structures were used, and Table 2 lists their references according to CN and spin. These references generally cover from 1969 to 1975. The cation radii were derived to a first approximation from these distances, and then adjusted to be consistent with both the experimental interatomic distances and radii–unit cell volume (r^3 *vs* V) plots, as in

* Polyhedral distortion was not considered in SP 69.

SP 69. Although such r^3 vs V plots are not always linear (Shannon, 1975), their regular curvilinear nature still allows prediction of radii. This system is particularly accurate for radii in the middle of a series, and least reliable for large polarizable cations like Cs^+ , Ba^{2+} , and Ti^{3+} . Radii-volume plots were used by Knop & Carlow (1974) and Fukunaga & Fujita (1973) to derive radii of tetravalent cations. These radii were used along with experimental interatomic distances in deriving the final radii. Greis & Petzel (1974) derived rare earth radii in eight- and nine-coordination using accurate cell dimensions for rare earth trifluorides and distances calculated using the structural parameters of YF_3 and LaF_3 . These radii were used in Table 1 after applying small corrections (+0.030 Å to ${}^{\text{IX}}\text{La}^{3+}$, ${}^{\text{IX}}\text{Ce}^{3+}$, ${}^{\text{IX}}\text{Pr}^{3+}$, and ${}^{\text{IX}}\text{Nd}^{3+}$; +0.025 Å to all other Greis & Petzel ${}^{\text{IX}}\text{RE}^{3+}$ radii, and 0.015 Å to all

${}^{\text{VIII}}\text{RE}^{3+}$ radii) for consistency with experimental interatomic distances and radii-CN plots.

Where structural data were not available or not accurate, plots of (1) radii vs unit cell volumes, (2) radii vs CN and (3) radii vs oxidation state, or combinations of these were used to obtain estimated values. Fig. 1 shows examples of radii-valence plots used to provide consistency between experimental radii and those anticipated from the regular nature of these plots. Cations whose final radii values were derived from both estimated values and experimental interatomic distances are: ${}^{\text{VI}}\text{Os}^{5+}$, ${}^{\text{VI}}\text{Os}^{6+}$, ${}^{\text{VI}}\text{Os}^{7+}$, ${}^{\text{VI}}\text{Re}^{4+}$, ${}^{\text{VI}}\text{Re}^{5+}$, ${}^{\text{VI}}\text{Re}^{6+}$, ${}^{\text{VI}}\text{Re}^{7+}$, ${}^{\text{VI}}\text{Rh}^{4+}$, ${}^{\text{VII}}\text{U}^{4+}$, ${}^{\text{VII}}\text{U}^{5+}$, and ${}^{\text{VII}}\text{U}^{6+}$.

Fig. 2(a)-(e) shows plots of radii vs CN. Generally, it was assumed that radii-CN plots for two different ions do not cross. Radii for ${}^{\text{IV}}\text{Cu}^+$, ${}^{\text{VI}}\text{Cu}^+$, ${}^{\text{IX}}\text{Rb}^+$, ${}^{\text{VII}}\text{Ni}^{2+}$, ${}^{\text{VII}}\text{Er}^{3+}$, ${}^{\text{VII}}\text{Yb}^{3+}$, ${}^{\text{VII}}\text{Tb}^{3+}$, ${}^{\text{XII}}\text{Nd}^{3+}$, ${}^{\text{IV}}\text{Cr}^{4+}$,

Table 1. Effective ionic radii

CR crystal radius, IR effective ionic radius, R from r^3 vs V plots, C calculated, E estimated, ? doubtful, * most reliable, M from metallic oxides.

ION	EC	CN	SP	CR	'IR'	ION	EC	CN	SP	CR	'IR'	ION	EC	CN	SP	CR	'IR'
AC+3 6 VI		1.26	1.12	R		CL-1 3P 6 VI		1.67	1.81	P		GD+3 4F 7 VII		1.14	1.00		
AG+1 4D10 II		.81	.67			CL+5 3S 2 IIIPY	.26	.12	*		VIII		1.193	1.053 R			
IV		1.14	1.00	C		CL+7 2P 6 IV	.22	.08			IX		1.247	1.107 RC			
IV VSQ		1.16	1.02			V	.76	.44			X		1.271	1.137 R			
V		1.23	1.09	C		CH+3 5F 7 VI	.41	.27	A		GE+2 4S 2 VI	.87	.74				
VI		1.29	1.15	C		CH+4 5F 6 VI	.99	.85	R		GE+4 3D10 IV	.530	.390 *				
VII		1.36	1.22			VIII	1.09	.95	R		VI		.670	.530 R*			
VIII		1.42	1.28			CD+2 3D 7 IV	.72	.58			H+1 1S 0 I		.24	.18			
AG+2 4D 9 IV VSQ		.93	.79			V	.81	.67	C		II		.04	.18			
VI		1.00	.94			VI	.76	.62	R		IV		.72	.51	R		
AG+3 4D 8 IV VSQ		.81	.67			HS	.885	.745	R*		VII		.90	.76			
VI		.89	.75	R		VIII	1.04	.90			VIII		.97	.83			
AL+3 2P 6 IV		.53	.39	*		CD+3 3D 6 VI	LS	.685	.545	R*		HG+1 6S 1 III	1.11	.97			
V		.62	.48			VII	.75	.61			VI		1.33	1.19			
VI		.675	.535	R*		CD+4 3D 5 VI	HS	.75	.64			HG+2 5D10 I	1.10	.96			
AM+2 5F 7 VII		1.35	1.26			VI	.67	.54	R		IV		.16	.02			
VII		1.40	1.26			CR+2 3D 4 IV	LS	.87	.73	E		VII		1.28	1.14	R	
IX		1.45	1.31			HS	.94	.80	R		VIII		1.041	.901 R			
AM+3 5F 6 VI		1.115	.975	R		CR+3 3D 3 VII	.755	.615	R*		VIII		1.155	1.015 R			
VII		1.23	1.09			CR+4 3D 2 IV	.55	.41			IX		1.212	1.072 R			
AM+4 5F 5 VI		.99	.85	R		VI	.69	.55	R		X		1.26	1.12			
VII		1.09	.95			CR+5 3D 1 IV	.485	.345	R		I -1 5P 6 VI	2.04	2.22	A			
AS+5 4S 10 IV		.475	.335	R*		VIII	.71	.57			I +5 5S 2 IIIPY	.58	.44 *				
VI		.60	.46	C		CR+6 3P 6 IV	.40	.26			VI		1.09	.95			
AT+7 5D10 VI		.76	.62	A		VI	.58	.44	C		I +7 4D10 IV	.58	.42				
AU+1 5D10 VI		1.51	1.37	A		CS+1 5P 6 VI	1.81	1.67			VII		.67	.53			
AU+3 5D 8 IV VSQ		.82	.68			VIII	1.88	1.74			IN+3 4D10 IV	.76	.62				
VI		.99	.85	A		X	1.92	1.70			VII		1.040	.900 R*			
AU+5 5D 6 I		.71	.57			XI	1.95	1.81			VIII		1.06	.92	RC		
d +3 LS 2 III		.15	.01	*		XI	1.99	1.85			IR+3 50 6 VI	.82	.68	E			
IV		.25	.11	*		XII	2.02	1.88			IR+4 50 5 VI	.765	.625 R				
VI		.41	.27	C		CU+1 3D10 II	.60	.46			IR+5 50 4 VI	.71	.57	EM			
BA+2 5P 6 VI		1.49	1.35			IV	.74	.60	E		K+1 3P 6 IV	1.51	.37				
VII		1.56	1.38	C		VII	.91	.77	E		VII		1.52	1.34			
VIII		1.61	1.42			CU+2 3D 9 IV VSQ	.71	.57	*		VII		1.50	1.36			
IX		1.66	1.52			VII	.79	.65	*		VIII		1.65	1.51			
XI		1.71	1.57			VIII	.87	.73			IX		1.69	1.55			
XII		1.75	1.61	C		CU+3 3D 8 VI	LS	.68	.54			XI		1.73	1.59		
BE+2 1S 2 III		.20	.16			D+1 1S 0 I	.04	.10			VI		1.78	1.64			
VI		.41	.27	*		DY+2 4F10 I	1.1	.17			VII		1.782	1.632 R			
VII		.59	.45	C		VIII	1.22	.13			VIII		1.24	1.17			
BI+3 6S 2 V		1.10	.96	C		VIII	1.33	.19			VII		1.300	1.160 R			
VI		1.17	1.03	R*		UY+3 4F 9 VI	1.052	.912	R		IX		1.356	1.216 R			
VIII		1.31	1.17	R		VII	1.11	.97			X		1.41	1.27			
BI+5 5D10 VI		.90	.76	E		VIII	1.157	1.027	R		XI		1.50	1.36 C			
BK+3 5F 8 VI		1.10	.94			VII	1.15	1.030	R		VI		.90	.70 *			
BK+4 5F 7 VI		.97	.83	R		VIII	1.030	.890	R		VII		1.06	.92 C			
VII		1.07	.93	R		VII	1.085	.945			VIII		1.001	.861 R			
BR-1 4P 6 VI		1.82	1.96	P		VIII	1.144	1.004	R		VII		1.117	.977 R			
BR+3 4P 2 IV VSQ		.73	.59			IX	1.202	1.062	R		IX		1.172	1.032 R			
BR+5 4S 2 IIIPY		.45	.31			VII	1.31	.17			VII		.71	.57			
BR+7 3D10 IV		.39	.25			VII	1.34	.20			VII		.80	.620 *			
VII		.53	.37	A		VIII	1.39	.25			VIII		1.03	.89 G			
C +4 1S 2 III		.06	-.08			X	1.44	.130			VI		.80	.66			
IV		.29	.15	P		XI	1.49	.135			V		.89	.75 C			
VI		.30	.16	A		EU+3 4F 6 VI	1.087	.947	R		VI		.81	.67 E			
VII		.30	.16			VII	1.15	.101			VII		.970	.830 R*			
VIII		.20	1.06	*		VIII	1.206	1.066	R		VII		1.04	.96 C			
VII		1.26	1.12	*		IX	1.260	1.120	R		VII		1.10	.96 R			
IX		1.32	1.18			VII	1.145	1.095	R		VIII		.72	.58			
X		1.37	1.23	C		VII	1.16	1.130			VII		.72	.58			
XII		1.48	1.34	C		IV	1.17	1.31			VII		.72	.58 R			
CD+2 4D10 IV		.92	.78			VII	1.19	1.33			VI		.785	.665 R*			
V		1.01	.87			VII	.22	.08	A		VII		.53	.39 R			
VI		1.09	.95			VII	.77	.63			VII		.70	.530 R*			
VII		1.17	1.03	C		VII	.78	.64			VII		.43	.33 R			
VIII		1.24	1.10	C		VII	.75	.61	E		MN+6 3D 1 IV	.395	.255				
XII		1.45	1.31			VII	.920	.780	R		MN+7 3P 6 IV	.39	.25				
CE+3 6S 1 V		1.15	1.01	R		VIII	1.06	.92	C		VII		.60	.46 A			
VII		1.21	1.07	E		VII	.63	.49	*		MN+3 4D 3 V	.83	.69 E				
VII		1.21	1.07	E		VII	.72	.58			MN+4 4D 2 V	.790	.650 R				
VIII		1.283	1.143	R		VII	.69	.55	R		MN+5 4D 1 V	.40	.34 R				
IX		1.36	1.26	R		VII	.785	.645	R		VII		.75	.61 R			
X		1.39	1.25			VII	.92	.78			VII		.55	.41 R*			
XII		1.48	1.34	C		VIII	.725	.585	R		VII		.65	.50			
CE+4 5P 6 VI		.01	.87	R		VII	.39	.25	R		VII		.73	.59 R*			
VII		1.11	.97	R		VII	1.94	1.08			VII		.47	.37 R			
X		1.21	1.07			VII	.61	.47	*		N -3 2P 6 V	1.32	1.16				
XII		1.21	1.07			VII	.69	.55			N +5 1S 2 III	.30	.16 A				
CF+3 6D 1 V		.109	.95	R		VII	.760	.620	R		VII		.044	-.104			
CF+4 5P 8 VI		.961	.821	R		VII	1.070	.938	R		VII		.27	.13 A			

Table 1 (cont.)

ION	EC	CN	SP	CR	*IR*	ION	EC	CN	SP	CR	*IR*	ION	EC	CN	SP	CR	*IR*
NA+1 2P 6 IV		1.13	.99			PR+3 4F 2 VI		1.13	.99	R		TC+4 4D 3 VI		.785	.645	RM	
V	1.14	1.00				VIII	1.266	1.126	R	TC+5 4D 2 VI		.74	.60	ER			
VI	1.16	1.02				IX	1.319	1.179	R	TC+7 4P 6 IV		.51	.37				
VII	1.26	1.12				X	1.39	1.09	R	VII		.70	.54	A			
VIII	1.32	1.18				VIII	1.10	.94	R	TE-2 5P 6 VI		2.07	2.21	P			
IX	1.38	1.24	C			VI	.74	.60		TE+4 5S 2 III		.66	.52				
XII	1.53	1.39				VII	.94	.80	A	IV		.80	.66				
NB+3 4D 2 VI	.86	.72				VI	.765	.625	R	VII		1.11	.97				
NB+4 4D 1 VI	.82	.68	RE			VII	.71	.57	ER	IV		.57	.43	C			
NB+5 4P 6 IV	.93	.78				VIII	1.14	1.00	R	VII		.70	.54				
NB+5 4P 6 IV	.92	.78	C			VI	1.10	.94	R	VII		1.08	.94	C			
VII	.78					VIII	1.10	.94	R	VIII		1.19	1.05	RC			
VII	.83	.69	C			VI	.88	.74	E	IX		1.23	1.09	*			
VII	.88	.74				VII	.85	.71	R	X		1.27	1.13	E			
ND+2 4F 4 VIII	1.43	1.29				XI	1.62	1.46	R	XI		1.32	1.18	C			
ND+3 4F 3 VIII	1.23	1.03	R			XII	1.84	1.70	R	XII		1.35	1.21				
ND+3 4F 3 VIII	1.23	1.03	R			VI	1.46	1.36	R	TI+2 3D 2 VI		1.00	.86	E			
IX	1.29	1.09	R			VII	1.70	1.56		TI+3 3D 1 VI		.810	.670	R*			
IX	1.303	1.163	R			VIII	1.75	1.61		TI+4 3P 6 IV		.56	.42	C			
XII	1.41	1.27	E			IX	1.77	1.63	E	V		.65	.51	C			
NI+2 3D 8 IV	.69	.55				X	1.80	1.66		VII		.745	.605	R*			
IV	.63	.49				XI	1.83	1.69		VIII		.68	.54				
IVSQ	.63	.49				XII	1.86	1.72		VII		1.54	1.50	R			
VII	.77	.63	E			VI	1.97	1.83		VIII		1.73	1.59	R			
VI	.830	.690	R*			VII	.77	.63	RM	VII		1.84	1.70	RE			
NI+3 3D 7 V	LS	.70	.56	E		VIII	.72	.58	E	TL+3 5D 10		.89	.75				
HS	.74	.60	E			IX	.69	.55	E	VII		1.025	.885	R			
NI+4 3D 6 VI	LS	.62	.48	R		XI	1.52	1.37	R	VIII		1.12	.98	C			
ND+2 5F 4 VI	1.24	1.11	E			XII	1.66	1.51	R	TM+2 4F 13		.77	.63				
ND+2 5F 5 VI	1.24	1.10	R			VI	1.70	1.56		VII		1.23	1.09				
NP+3 5F 3 VI	1.15	1.01	R			VIII	.805	.645	R	VIII		1.020	.880	R			
NP+4 5F 3 VI	1.01	.87	R			IX	.74	.60	RM	VII		1.130	.99	R			
NP+5 5F 2 VI	.89	.75				XI	.69	.55		IX		1.192	1.052	R			
NP+6 5F 1 VI	.86	.72	R			XII	.82	.68		U+3 5F 3 VI		1.165	1.055	R			
NP+7 6P 6 VI	.85	.71	R			VI	.760	.620	RM	U+4 5F 2 VI		.89	.75				
D-2 2P 6 VI	1.21	1.15	R			VII	.705	.565	ER	VII		1.09	.95	E			
IV	1.21	1.15	R			VIII	.52	.42		VIII		1.14	1.00	R*			
VII	1.22	1.16	R			IX	.50	.36		XI		1.19	1.05				
VII	1.24	1.18	S-2 3D 6 VI			XII	1.70	1.54	P	XII		1.31	1.17	E			
VII	1.26	1.40	S+6 3S 2 VI			VI	.51	.37	A	U+5 5F 1 VI		.90	.76				
OH-1	1.18	1.32	S+6 2P 6 IV			VII	.43	.29	C	VII		.59	.45	E			
III	1.20	1.34	SB+3 5S 2 IV			VIII	.50	.36		U+6 6P 6 I		.66	.52				
IV	1.21	1.35	SB+3 5P 2 IV			IX	.94	.80		VII		.87	.73	*			
VII	1.23	1.37	SB+3 5E 2 IV			XI	.90	.76	A	VII		.95	.81	E			
DS+4 5D 4 VI	.770	.630	RM			XII	.74	.60	*	VIII		1.00	.86				
DS+5 5D 3 VI	.715	.575	E			VI	.885	.745	R*	V+2 3D 3 VI		.53	.39				
DS+6 5P 6 IV	.63	.49				VII	1.010	.870	R*	V+3 3D 2 VI		.780	.640	R*			
DS+7 5O 1 VI	.685	.545	E			VIII	1.084	1.06	P	V+4 3D 1 V		.67	.53				
DS+8 5P 6 IV	.53	.39				IX	.42	.28	*	V		.72	.58	R*			
P+3 3S 2 VI	.58	.44	A			XI	.56	.42	C	VIII		.86	.72	E			
P+5 2P 6 IV	.31	.17	*			XII	.40	.26	*	V		.60	.46	*			
V	.43	.29				VI	.540	.400	R*	V		.54	.40				
PA+3 5F 2 VI	1.18	1.08	S+M+2 4F 6 VI			VII	1.36	1.24		V		.60	.46				
PA+4 6D 1 VI	1.04	.90	R			VIII	1.41	1.29		VI		.54	.40				
PA+5 6D 1 VI	1.15	1.01	SM+3 4F 5 VI			IX	1.46	1.32		W+5 5D 2 VI		.80	.66	RM			
PA+6 6P 6 VI	.92	.78				XI	1.16	1.02	E	W+5 5P 6 IV		.76	.62	R			
VII	1.05	.91				XII	1.219	1.079	R	V		.65	.51				
IX	1.09	.95				VI	1.272	1.132	R	VII		.74	.60	*			
PB+2 6S 2 IV	1.12	1.09	C			VIII	1.38	1.24	C	VII		.62	.48				
VII	1.23	1.19	SN+4 4D 10 IV			IX	.76	.62	C	Y+3 4P 6 VI		1.040	.900	R*			
VII	1.37	1.23	C			XI	.830	.690	R*	VII		1.10	.96				
VII	1.43	1.29	C			XII	.89	.75		VIII		1.150	1.019	R*			
IX	1.49	1.35	C			VI	.95	.81	C	YB+2 4F 14 VI		1.215	1.075	R			
X	1.54	1.40	C			VII	1.16	1.10		VII		1.16	1.04				
XI	1.59	1.45	C			VIII	1.32	1.16		VII		1.22	1.08	E			
XII	1.63	1.49	C			IX	1.15	1.11		VIII		1.28	1.14				
PB+4 5O 10 IV	.79	.65	E			XI	1.40	1.26		YB+3 4F 13 VI		1.008	.868	R*			
V	.87	.73	E			XII	1.45	1.31		VII		1.065	.925	E			
VII	.915	.775	R			VI	.76	.62		VIII		1.125	.985	R			
VII	1.08	.94	R			VII	.830	.690	R*	IX		1.182	1.042	R			
PD+1 4D 9 II	.73	.59				XI	1.58	1.44	C	YB+2 4F 14 VI		.82	.68	*			
PD+2 4D 8 IV	.78	.64				XII	.86	.74	E	ZN+2 3D 10 IV		.880	.740	R*			
PD+2 4D 8 IV	1.00	.86				VI	.82	.68		V		.82	.68	*			
PD+3 4D 7 V	.90	.76				VII	.78	.64		VII		.98	.84	*			
PD+4 6D 6 VI	.755	.615	R			VIII	.83	.69		VIII		1.04	.90	C			
PM+3 4F 4 VI	1.11	.97	R			IX	.88	.74		ZR+4 4P 6 IV		.73	.59	R			
VII	1.233	1.093	R			XI	1.063	.923	R	V		.80	.66	C			
IX	1.284	1.044	R			VII	1.12	.98	E	VII		.96	.82	R*			
PO+4 6S 2 IV	1.05	.99	R			VIII	1.180	1.040	R	VII		.92	.78				
VII	1.22	1.08	R			IX	1.235	1.095	R	VIII		.98	.84	*			
PD+6 5D 10 VI	.81	.67	A			XI	1.00	.90	R	VII		1.03	.89				

^{VIII}V⁴⁺, ^{IV}Pb⁴⁺, and ^XTh⁴⁺ obtained from these plots were used to help determine the values in Table 1. The first estimate of ^{VIII}V⁴⁺ was made from distances in C₃₂H₂₈S₈V (Bonamico, Dessim, Fares & Scaramuzza, 1974).

Another method used to estimate radii was based on the empirical relationship between interatomic distances and bond strengths. Brown & Shannon (1973) derived these relationships for the cations in the first three rows of the periodic table from a large number of experimental interatomic distances. These curves can be used to calculate hypothetical distances for cations in any coordination (Brown & Shannon, 1973; Shannon, 1975; Brown, 1975). Examples of cations whose radii were calculated in this way are: ^{IV}Mn²⁺, ^{VI}Be²⁺, ^{VI}B³⁺, ^{VI}Pb⁵⁺, ^{VI}S⁶⁺, ^{VIII}Mg²⁺, and ^{VIII}Fe²⁺. These are marked with a C in Table 1. In certain cases, these values were combined with known structural data (see Table 2) to obtain the radii in Table 1. Although the

majority of radii were derived from oxides and fluorides,* some were taken from chlorides, bromides, iodides, and sulfides. For large electropositive cations with highly ionic bonds, very little covalent shortening is believed to occur and radii derived from these other compounds should differ only slightly from those derived from fluorides and oxides. Examples are divalent rare earths such as Yb²⁺, Tm²⁺, Dy²⁺, Sm²⁺, Nd²⁺ and the ions Am²⁺, Ac³⁺, Np³⁺, and U⁴⁺.

Another useful scheme for estimation of radii is the comparison of unit-cell volumes of compounds containing cations of similar size. McCarthy (1971) prepared a number of isotropic Sr²⁺ and Eu²⁺ ternary oxides and generally found the unit cells of the Sr²⁺

* Because of covalency differences in M-O and M-F bonds, oxide distances were emphasized. Therefore the radii in Table 1 are more applicable to oxides than fluorides. This subject is treated further in the discussion *Effects of covalence*.

Table 2. *References for Table 1*

The references here and in Tables 4, 5, 6 and 8 are abbreviated according to *Codens for Periodic Titles* (1966).

Table 2 (cont.)

74 ZAACCA 403 1 R3 VS V (DY F3)	73 ACBCA 29 869 MG NO D4	74 AGCHA 30 2691 MG2 V2 O7
ER+3 VI 10 ZACBCA 26 484 ER2 S12 O7	74 ACBCA 30 2049 K NO BE F4	71 AMMIA 56 1553 MG (B6 DT IO M16).2HZ U
ER+4 VII 10 ZACBCA 26 484 ER2 S12 O7	70 ZACBCA 8 1745 HD3 FES D12	73 AMMIA 58 1029 MG C O3
70 SPMCA 15 38 ER2 GEZ D7	72 BUFCFA 95 437 HD5 P5 D14	70 CJCHA 52 1801 MG2 S12 H2 (P D6)14
72 JCHMLB 2 197 ER8 U (THD10 (O) H12	73 ZAACCA 403 1 R3 VS V (HU F3)	70 INOCA 151 MG (C9P4)3 (C)
ER+5 VIII 10 ZACBCA 2 47 ER P 04, ER V 04	HOD+3 IX 73 ZAACCA 403 1 R3 VS V (HU F3)	72 CJCHA 50 3619 MG2 V2 U6
70 INOCA 9 2100 ER (C2 D4) (H C2 O4).JH2 O	74 ACBCA 30 2613 HOIC2 M5 S ON13.9HZ O	73 ACBCA 29 2611 MG3 AS2 O8
70 SSCOA 8 1745 ER3 FES O12	HOD+3 X 74 INOCA 13 2595" HO(H O14 (M C O3)3.2HZ O	HG2+ VIII 29 266 CALCULATED
71 ACSAA 25 372 ER (H O C H2 C O O13.2HZ O	74 ACBCA 54 2556 N H4 I D3	MN+2 IV 70 AMMIA 55 1489 MN7 SB A5 O12
74 ZAACCA 403 1 R3 VS V (ER F3)	66 ACCRA 20 758 L1 I 03	69 ZACBCA 369 306 MN V2 O4
72 JCHMLB 2 197 ER8 U (THD10 (O) H12	66 ACCRA 20 854 L1 I 03	69 PHSSA 32 K91 MN CR2 D4
ER+3 IX 59 ZKKKA 112 J66 IC2 M5 S O4)3.9HZ O	66 ACCRA 11 854 L1 I 03	73 ACACB 29 266 CALCULATED
74 ZAACCA 403 1 R3 VS V (ER F3)	58 ACCRA 11 794 CE II O3)4..H2 O	MN+2 V HS
EU+2 VI 70 ZAACCA 374 201 L1 EU3 O4	43 RTCPA 62 729 N H4 I 03	74 AMMIA 53 1841 MN2 O H A5 O4
EU+2 VII 70 ZAACCA 374 201 L1 EU3 O4	I+7 VI 70 JCPSCA 54 2556 N H4 I 03	74 AMMIA 54 1246 MN2 AS D4 O4
69 ACBCA 25 1104 EU12	70 ACBCA 26 1782 NA I 04	74 AMMIA 21 246 MN2 AS D4 O4
73 REF 3 129 EU12	26 ZEPYA 39 308 K 1 04	MN+2 VI LS
EU+2 VIII UNPUI EU F2, EU BR2	70 JCSIA 1971 1837 I(+7)-U	69 ACBCA 25 925 R VS D ELECTRONS
EU+2 IX UNPUI EU F2, EU BR2	I+7 VII 70 ACBCA 54 2556 N H4 I 03	MN+2 VII 69 SC15 165 586 MN2 GE U4
EU+2 X 73 RVMCA 10 76 CL2	70 ACBCA 26 1782 NA I 04	69 JCPSCA 51 4928 BA MN F4
EU+2 XI UNPUI EU F2	26 ZEPYA 39 308 K 1 04	70 ZKKKA 132 MN5 (O) H12 S12 O8
EU+2 XII 71 NATWA 58 218 EU2 S1 U4	70 JCSIA 1971 1837 I(+7)-U	69 AMMIA 54 1311 MG2 FE2 (P D4)2.10H12.8HZ O
68 REF 4 EU AL2 D9	I+7 VIII 66 ACCRA 20 765 H5 I U6	69 ACCRA 18 854 MN S 04
70 ZAACCA 374 201 L1 EU3 O4	65 ACCRA 19 649 K4 H2 12 D10.8HZ O	72 AMMIA 57 621 MN2 GE O4
73 REF 3 129 EU12	65 ACCRA 59 2036 IN H4(2) H3 I U6	67 PRLAA 92 125 MN C O3
EU+3 VII 68 JCPSCA 48 1094 EU3 FE2 GAZ O12	I+7 IX 74 ZAACCA 409 97 R82 IN4 O7	67 PRLAA 50 2023 MN5 O8
74 ZAACCA 403 1 R3 VS V (EU F3)	73 ZAACCA 395 280 SR2 IR2 D5	MN+2 X 72 AMMIA 57 621 MN2 GE O4
EU+3 VIII 73 ZAACCA 26 1782 NA I 04	I+7 X 74 ZAACCA 409 97 R82 IN4 O7	MN+2 VIII 70 AMMIA 129 427 MN1 FE2 GE3 O12
68 JCPSCA 27 2827 EU (C3 H2 O4)3.8HZ O	71 ACSAA 15 1437 IN O M S O4.(H2 O12	71 AMMIA 56 791 GARNETS
73 ACSAA 27 2827 EU (C3 H2 O4)3.8HZ O	68 ACBCA 24 388 CU2 IN2 O5	73 SSCOA 12 109 MN3 AL2 GE3 O12
74 ZAACCA 403 1 R3 VS V (EU F3)	70 ACSAA 24 1662 IN O H	74 JCPSCA 60 1899 MN4 B4 O7
73 ACSAA 27 2827 EU (C3 H2 O4)3.8HZ O	70 ACSAA 24 1662 IN O H	MN+2 IX 67 ACSAA 21 2871 MN2 D3
74 ZAACCA 403 1 R3 VS V (EU F3)	70 SPHDA 18 761 IN2 GE2 O7	67 ZKKKA 124 428 MN2 D3
73 ACSAA 27 2827 EU (C3 H2 O4)3.8HZ O	I+7 XI 70 JSSCB 3 174 SR IR 03	68 ACRCRA 24 1233 MN O O H
71 ACSAA 25 3347 EU TRISGLYCOLATE	I+7 XII 70 MRBUA 9 1177 R3 VS V (CO2 IR2 O7)	69 JCPSCA 30 1064 MN2 D12 MN F5
71 ACSAA 25 3347 EU TRISGLYCOLATE	K+1 IV 60 ZAACCA 165 245 K AG 02	70 MRBUA 13 1864 MN (ACAC13)
71 IV SS HS 74 ZAACCA 59 1166 BA FE 010	60 ZAACCA 165 245 K AG 02	MN+4 IV 70 JSSCB 3 238 LA MN O3, MM MN O3,
FE+2 IV SS HS 69 NJMHA 1969 430 FE AL2 (P D4)2 IO H12 (O) H216	71 ZAACCA 9 345 K FE 02	LA-95, CA05 MN O3,
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	K+1 V 70 ZAACCA 26 1782 NA I 04	70 JSSCB 6 165 MN O3
69 ZAACCA 367 308 FE V2 O4	61 ACSAA 15 1437 IN O M S O4.(H2 O12	70 INOCA 59 982 MG2 MN B5
71 ACSAA 367 308 FE V2 O4	68 ACBCA 24 388 CU2 IN2 O5	68 ACBCA 26 1114 MN4 MN4 T15 O18
72 JUPSA 33 1296 FE2 MD O4	70 ACSAA 24 1662 IN O H	70 INOCA 13 1854 MN IC7 H2 D213+1/4 C6 H5 CH3
FE+2 VI LS 69 ACBCA 25 925 R VS A (FE S2)	70 SPHDA 18 761 IN2 GE2 O7	70 INOCA 13 1864 MN (ACAC13)
FE+2 VII 69 NJMHA 1969 430 FE AL2 (P D4)2 IO H12 (O) H216	I+7 XIII 70 JSSCB 3 174 SR IR 03	MN+4 V 70 JSSCB 13 275 R3 VS V (MN MN O4)
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XIV 70 MRBUA 9 1177 R3 VS V (CO2 IR2 O7)	70 JSSCB 8 234 BA MN O3
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	K+1 V 60 ZAACCA 165 245 K AG 02	69 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 26 1782 NA I 04	69 CZYPA 13 398 MN7 H4 MN (I D6)3.17HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 117 411 K2 T16 O13	67 HOCACA 50 2023 MN5 O8, CO2 MN3 O8
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 26 1782 NA I 04	MN+4 VI 70 JSSCB 26 2845 K2 MN O4
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	74 ZAACCA 18 761 K2 T16 O13	68 ACBCA 24 1053 AG MN O4
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XV 70 JSSCB 8 234 BA MN O3	69 ACBCA 25 400 KJ MO CL6
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 345 K FE 02	69 INOCA 8 2694 K3 MO F6
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	K+1 VI 70 ZAACCA 132 27 K14 N45.5 CA0.3 ALT-5	69 MRBUA 6 555 L12 MO F6
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	18 L15-S 032	MN+4 VII 70 INOCA 13 2715 R3 VS V (RE H0 D4)
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	69 ACBCA 25 600 K C E F4	70 INOCA 10 922 B42 ND M0 D6
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	69 ACBCA 25 1919 K2 F2 U2	MN+4 VIII 68 SPHDA 12 1095 K Y MO D8
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	K+1 VII 70 ZAACCA 74 3006 K2 P D4	68 SPHDA 12 1095 K Y MO D8
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 117 411 K2 T16 O13	72 ACBCA 26 60 G02 MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 98 266 K2 H M13 O13 010	69 JCPSCA 50 86 N02 MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 INOCA 7 873 K H2 C2 O4	71 SPHDA 15 61 L13 FE MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 INOCA 7 873 K H2 C2 O4	71 SPHDA 15 61 L13 FE MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 117 411 K2 T16 O13	71 JCPSCA 55 1093 CA NO 04 SR MO 04
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 JSSCB 1970 3092 AU (IN 0316	73 ACBCA 29 2074 LA2 MO3 O12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	65 ACCRA 16 2692 K4 H2 12 D10.8HZ O	JCSIA 1971 1857 MO(+1)-0
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XVI 70 ZAACCA 132 27 K14 N45.5 CA0.3 ALT-5	MN+4 IX 67 CCJDA 1967 374 K2 MO3 D10
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	18 L15-S 032	68 JCPSCA 16 2692 K4 H2 12 D10.8HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	69 ACBCA 25 1919 K2 F2 U2	70 INOCA 12 1095 K Y MO D8
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	70 ZAACCA 117 411 K2 T16 O13	72 ACBCA 26 60 G02 MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	69 JCPSCA 50 86 N02 MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 AMMIA 56 18 NA3 L12 F13 P12	71 SPHDA 15 61 L13 FE MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 26 1782 NA I 04	71 SPHDA 15 61 L13 FE MO3 D12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 JSSCB 26 1782 NA I 04	71 JCPSCA 55 1093 CA NO 04 SR MO 04
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	74 ZAACCA 16 2692 K4 H2 12 D10.8HZ O	73 ACBCA 29 2074 LA2 MO3 O12
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XVII 70 ZAACCA 165 245 K AG 02	JCSIA 1971 1857 MO(+1)-0
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	MN+4 X 67 CCJDA 1967 374 K2 MO3 D10
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	68 JCPSCA 16 2692 K4 H2 12 D10.8HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XVIII 70 ZAACCA 165 245 K AG 02	69 CZYPA 13 398 MN7 H4 MN (I D6)3.17HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	67 HOCACA 50 2023 MN5 O8, CO2 MN3 O8
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	MN+4 X 70 JSSCB 8 234 BA MN O3
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	69 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XIX 70 ZAACCA 165 245 K AG 02	70 JSSCB 8 234 BA MN O3
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XX 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXI 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXII 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXIII 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXIV 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXV 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXVI 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXVII 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXVIII 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXIX 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	71 ZAACCA 9 1096 YB L1 F4	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	72 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	73 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.50HZ O
70 ZAACCA 166 1399 (NA)X12 FE4 S112 D30.8HZ O	I+7 XXX 70 ZAACCA 165 245 K AG 02	70 INOCA 8 335 H12 MN2 D12 D38.5

Table 2 (cont.)

PB+2 VII	70 ACACB	26 501 PB2 D3	50+3 IV	70 ACSAA	24 320 SB P 06
69 ZKAKA	128 213 PB CA2 S13 09	S8+5 VI	70 AMHIA	55 1480 RHT SB AS 012	
70 ACACB	26 501 PB2 D3	71 JCSIA	1971 942 AS SR F#		
PB+2 VIII	71 SPHCA	15 928 PB W D4	71 JCSIA	1971 2318 HRZ SB3 F16	
64 ACCRA	17 1539 PB P2 D6	74 JCSISB	9 345 NA SB 03		
70 ACACB	26 501 PB2 D3	S1+3 V	64 CJCMA	46 1446 SC2 O3	
71 UNPUL	3 93 NA3 NB3 ND4	68 ARKEA	29 343 SC2 O3		
ND+2 IX	ND 12	UNPUL	70 AMHIA	17 749 SC2 O3	
UNPUL	ND CL2, ND BR2	73 INDCA	12 927 SC IC3 HT 0213		
ND+3 X	ND 12	73 INDCA	29 2615 NA SC S12 O6		
INDCA	10 922 RA2 ND MD 06	74 INDCA	13 151 SC IC7 M5 D23		
MRAUA	9 1661 ND AL3 D12	73 INDCA	27 2841 SC U H IC3 H04.1-ZH2 O		
ND+4 XI	50 86 ND2 M03 012	64 SPHDA	14 9 943 SC S12 O7		
JSSCB	3 458 ND V M04	S6+3 VIII	70 AMHIA	10 137 SC H IC7 M5 D234	
SPHCA	14 1264 K ND M2 D0	71 AMHIA	26 1486 SC2 O3		
ACBCA	26 3404 R2 S12 D11	70 AMHIA	11 1886 SC2 O3		
SPHDA	15 636 ND2 W D6	71 AMHIA	12 1886 SC2 O3		
SPHCA	19 994 ND2 M3 018	70 AMHIA	13 1886 SC2 O3		
MRAUA	9 128 ND P5 D14	70 AMHIA	27 2841 SC U H IC3 H04.1-ZH2 O		
ACBCA	40 2972 ND OH M3 F31	64 ACBCA	29 343 SC S12 O7		
ACBCA	30 468 ND P3 09	71 JCSIA	1971 1857 SE1+01-O		
ND+3 IX	70 ACSAA	24 2860 ND2 IC2 D413.10.5H2 O	S1+4 IV	64 NATHA	50 91 FE2 S1 O4
SPHCA	12 991 ND2 M3 D15	73 ZKAKA	137 86 MG2 SI1 O4		
JCSAA	27 2441 ND2 IC2 H043.1-BH2 O	61 ACCRA	14 835 MG3 AL2 S13 O12		
ZKAKA	403 1 128 N2 V (ND F31)	70 AMHIA	12 1886 SC2 O3		
ACBCA	27 2813 ND2 IC3 H043.1-HM2 O	70 AMHIA	13 1886 SC2 O3		
ZKAKA	37 2972 ND OH M2 D0	70 AMHIA	27 2841 SC U H IC3 H04.1-ZH2 O		
AMHIA	59 1277 ND2 M02 T13 S14 D22	69 ACBCA	29 343 SC S12 O7		
JSSCB	4 11 ND AL D3	71 JCSIA	1971 1857 SE1+01-O		
NIC+2 V	52 685 N1 CR2 D4	S1+4 V	64 NATHA	50 91 FE2 S1 O4	
JAPIA	32 685 N1 CR2 D4	73 ZKAKA	137 86 MG2 SI1 O4		
BSCFA	1965 1085 SPINELS	61 ACCRA	14 835 MG3 AL2 S13 O12		
NIC+2 V	5 1200 H1 (DPH12)	70 AMHIA	12 1886 SC2 O3		
NIC+2 V	67 BAPCA	15 47 N12 P2 D7	70 AMHIA	13 1886 SC2 O3	
NIC+2 VI	70 AMHIA	5 1200 H1 (DPH12)	70 AMHIA	27 2841 SC U H IC3 H04.1-ZH2 O	
ACBCA	30 1886 NI (PY N1 D16 (B F4)2	70 AMHIA	56 1222 NA16 K8 CA4 IS18 0201F-BH2 O		
ZKAKA	358 1286 NI SE D6	71 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
BAPCA	15 47 N12 P2 D7	69 MSAPA	2 31 LI 11 S12 D6,NA M S12 G		
ZKAKA	32 1886 NI SE D6	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	378 1289 SR2 NI TE 06	69 MSAPA	2 95 FE4.1 MN1.1 RG.8 CA1 S18		
PHSCA	416 RD NI F3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
PHSCA	438 10 110 H2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	70 1886 NI SE D6	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	17 1481 NI IC5 H7 0212.2H2 O	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	29 2761 NI SI F6,6H2 O	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	118 291 NI (H C D0 012-ZH2 O	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	61 291 NI (H C D0 012-ZH2 O	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
JCLMB	3 181 NI IC5 H7 0212.1C2 H5 M0 H12	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	29 2303 NI M1 08	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
NIC+1 V	405 167 M2 H1 NI F6	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
JCSIA	71 CHODA	27 2163 HO NI U3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
NIC+1 V	54 JCSAA	76 1499 NA NI D2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
NIC+1 V	67 STGCA	3 1 R3 VS V (FLUORIDES)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
JINCA	36 1561 K2 NI F6	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
NIC+1 V	70 AMHIA	13 2233 ESTIMATED	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
NIC+3 VI	68 JINCA	30 823 NM CL3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
NIC+3 VI	67 JINCA	3 327 ESTIMATED	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
NIC+3 VI	74 CJCHA	52 2175 R3 VS V	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
NIC+6 VI	R3 VS V (PEROVSKITES)	PT+4 VII	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
DS+7 VI	R3 VS V (PEROVSKITES)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
DS+8 IV	66 ACSAA	20 395 OS D4	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	29 1983 OS D4	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	19 157 OS D4	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
JCSIA	1971 1857 OS18+-D	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
P4+5 IV	70 AMHIA	R1(H-L1)+R(F1)-1+-04	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	28 2883 CO2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
CJCHA	46 605 CU2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
CJCHA	47 605 CU2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
INDCA	1345 CAZ2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	142 R2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	26 142 R2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	26 142 R2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	26 142 R2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
NJHIA	241 SR AL3 (P04)2 10 H15.2 H2 D	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	130 148 K2 ER2 (P04)2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	22 1822 NA ZR2 P2 D2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	22 1822 NA ZR2 P2 D2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	127 21 AL3 P2 D8,6H2 D	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	25 127 K2 H5 (P04)2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	1 120 ZN2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	87 2268 C23 H29 U5 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
JACSA	89 2270 C23 H29 U5 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	89 2270 C23 H29 U5 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	71 ZKAKA	30 1 P CL3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	72 C2CDA	1972 676 ET3 H (IC6 H0 D2)3 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	29 266 CALCULATED	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
P4+6 VI	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
AMHIA	3 327 R (P4+4)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
CJCHA	52 2175 R3 VS V	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
P4+5 VI	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	27 731 K2 PA03	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	67 JCSIA	1967 1429 K2 PA F7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
PB+2 IV	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
AMHIA	126 98 P0 S1 Q3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
PB+2 VI	70 AMHIA	29 266 CALCULATED	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
P4+6 VI	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
AMHIA	380 51 P CL3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	141 LU P04	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	29 141 LU P04	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	27 292 R2 P2 D4,2H2 U	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	27 292 R2 P2 D4,2H2 U	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	25 125 K2 H5 (P04)2	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ZKAKA	1 120 ZN2 P2 D7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	67 JCSIA	1967 2269 C23 H29 U5 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
JACSA	89 2270 C23 H29 U5 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	89 2270 C23 H29 U5 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	71 ZKAKA	30 1 P CL3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	72 C2CDA	1972 676 ET3 H (IC6 H0 D2)3 P	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	29 266 CALCULATED	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
P4+6 VI	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
AMHIA	3 327 R (P4+4)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
CJCHA	52 2175 R3 VS V	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
P4+5 VI	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
ACBCA	27 731 K2 PA03	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
ACBCA	67 JCSIA	1967 1429 K2 PA F7	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
PB+2 IV	70 AMHIA	5 1 R3 VS V (CD2 R2 U7)	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	
AMHIA	126 98 P0 S1 Q3	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M		
PB+2 VI	70 AMHIA	29 266 CALCULATED	70 AMHIA	56 1155 MG5.6 FE2 S13 D12,NG F D M	

Table 2 (cont.)

TG+1	72 ACBCA	28 956 BA TB 03	TI JINCA	33 2867 CR2 U 06	69 PHSSA	32 K91 ZN FEZ 06
TG+1	67 STBGA	3 1 R3 VS V (FLUORIDES)	72 ACBCA	28 3469 U 02 (O) H2	73 ACSAA	27 1561 ZN S 03-2 1/2HZ 0
TG+1	69 AGCIA	8 381 TC2 07	73 ACBCA	29 7 U F6	64 INOCA	3 245 ZN (OPM2
TG+1	71 ACBCA	380 146 TC2 07	U+0 VI		73 CICHA	51 1004 ZN2 V2 D7
TE+0	IV		72 ACBCA	28 3609 U 03	71 AMMIA	56 1147 ZN4 AS2 O8 (O) H2-2HZ 0
TE+0	IV		69 AGCIA	25 1551 H3 FE2 TE4 O12 CL	ZN+2 VI	
TE+0	IV		71 ACBCA	27 602 TI TE3 08, SN TE3 08, TE 02,	73 CICHA	43 1147 ZN2 P2 D7
TE+0	IV		71 ACBCA	27 608 U TE3 09	68 SPHCA	13 127 ZN W 04
TE+0	IV		71 ACBCA	27 608 U TE3 09	70 JSSCB	1 120 ZN2 P2 D7
TE+0	IV		71 ACBCA	27 608 U TE3 09	71 CICHA	49 3056 ZN3 V2 DB
TE+0	IV		71 JCS1A	1971 1857 TE1(+)-0	72 CICHA	25 1004 ZN2 V2 D7 (O) H2-2HZ 0
TE+0	IV		69 ZENBA	26 647 TE 06	73 CICHA	29 271 ZN2 SI F6-6HZ 0
TE+0	IV		70 MRBUA	5 199 MG3 TE 06	73 ACSAA	27 1561 ZN S 03-2 1/2HZ 0
TE+0	IV		69 ACSAA	23 3062 MA2 K4 TE2,08 (O) H2 (H2 O)14	ZR+4 IV	
TE+0	IV		64 INOCA	3 199 MG3 TE 06	75 JSSCB	13 275 R3 VS V (M4 ZA 04)
TE+0	IV		64 NATMA	51 552 K TE O D H	ZR+4 VI	
TE+0	IV		66 ACSAA	20 2138 K4 TE2 06 (O) H2-2HZ 0	69 CCJDA	1969 272 K2 ZR 03
TE+0	IV		70 NATMA	57 393 MG3 TE 06	70 JSSCB	2 410 K2 ZR 03
TE+0	IV		70 ACBCA	29 1535 H3 FE2 TE 06	ZR+4 VII	
TE+0	IV		70 ACBCA	26 3178 TE (O) H16	69 ACBCA	25 2658 ZR (M AS 04-12-H2 0
TE+0	IV		66 ACSAA	20 1535 TE F6	69 ZAAC	371 200 L12 ZR 03
TE+0	IV		71 ACBCA	27 615 MG3 TE 06	70 JSSCB	1 478 K2 ZR2 D5
TE+0	IV		65 ZAAC	3 199 MG3 TE 06	64 ACSAA	27 1561 ZN2 V2 D7
TE+0	IV		69 ACBCA	26 1532 TE 06	73 CICHA	29 2294 ZN2 F6
TE+0	IV		69 ACBCA	100 1809 AG2 TE 02 (O) H14	71 ACBCA	27 1944 RBS ZR4 F21
TE+0	IV		71 BUFEA	94 172 TE (O) H16	74 CICHA	52 2175 R3 V5 V
TE+0	IV		73 ACBCA	29 643 TE2 06	ZR+4 VIII	
TE+0	IV		73 ACBCA	29 1535 H3 TE2 06	69 ACBCA	25 2164 MA2 ZR F6
TE+0	IV		73 ACSAA	27 85 TE (O) H16	70 ACBCA	26 417 IN H13 ZR FT
TE+0	IV		74 ACBCA	30 1813 H2 TE 04	73 ACSAA	27 177 ZR4 (O) H16 (O) D4-15-H2 0
TE+0	IV		74 ACBCA	30 2095 (H M16 (TE MD6 024) TE (OH)6	73 CICHA	27 1561 ZN2 V2 D7
TH+4 VI			74 ACBCA	27 2275 TH F6	73 JSSCB	27 1944 RBS ZR4 F21
TH+4 VI			74 CICHA	52 2175 Y2 V 03	63 INOCA	2 250 NAK ZR (CZ 04-12-H2 0
TH+4 VI			74 CICHA	52 2175 Y3 VS V	KEF 1 G. E. BROOKS, PH.D., THESIS, VIRGINIA POLYTECH. INST., UNIV. MICHAEL MS., 78-498	
TH+4 XI			74 CICHA	52 2175 Y3 VS V	REF 2 R.W.G. WYCKOFF, CRYSTAL STRUCTURES, WILEY, N.Y., 1963	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	REF 3 J. H. HAUSEN ET AL., PROC. 10TH R.E. RES.-CONF., CAREFREE, ARIZ (1973)P-490	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	REF 4 C. BRANDELL & STEINFINK, PROC. 7TH R.E. RES.-CONF., CORONADO, CALIF., OCT 28-30, 1972	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	REF 5 G. E. BROOKS, PAT. 3,616,166, APR 16, 1972	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	REF 6 W.H. RAUB, NITROGEN-HANDBOOK OF GEUCHEN, SPRINGER-VERLAG, NY, 1974	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	REF 7 A.M. SLEIGHT, U.S. PAT. 3,645,154, NOV 19, 1974	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	UNPUB A.M. SLEIGHT, PERSONAL COMMUNICATION	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	UNPUB C. CALVO, PERSONAL COMMUNICATION	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	UNPUB C.T. PREWITT, PERSONAL COMMUNICATION	
TH+4 XII			74 CICHA	52 2175 Y3 VS V	UNPUB W.H. RAUB, PERSONAL COMMUNICATION	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ACAB ACTA CRYST. SECT. A	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ACBCA ACTA CRYST. SECT. B	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ACIEA ANGEM. CHEM. INT. ED.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ACCSA ACTA CRYST. SCAND.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ADCSA ADV. CHEM. SER.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ANCPA ANNLS CHIM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	ARKEA ARK. KEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	BAPCA BULL. ACAD. PUL. SCI. SER. SCI. CHIM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	BAPCA BULL. SOC. CHIM. FR.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	BUFCA BULL. SOC. FR. MINER. CRYSTALLOGR.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CAMIA CAN. MINERALIST	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CDCA CHEM. COMMUN.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CHDA C. H. HEBD. SEAN. ACAD. SCI. SER. B	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CHDA C. R. HEBD. SEAN. ACAD. SCI. SER. C	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CIVYA CARNEGIE INST. WASH. YEARBOOK	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CJCHA CAN. J. CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	CZCPA CZECH. PHYS. SOC.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	DANKA DOKL. AKAD. NAUK. SSSR	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	HECAA HELV. CHIM. ACTA	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	INDCA INORG. CHEM. ACTA	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	INDCA INORG. CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	INDRA RUSS. J. INORG. CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	INDUA INORG. NUCL. CHEM. LETT.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JACSA J. Z. ANGL. SOC. SSRR, NEORG. CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JAGCA J. APPL. CRYSTALLOGR.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JACTA J. AM. CERAM. SOC.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JAPCA JAP. CERAM. SOC.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JCLB J. XE. 06-072 O	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JCOMA J. LSS-COMMON METALS	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JCPSA J. CHEM. PHYS.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JCPSA J. SOLID STATE CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JSTCA J. STRUCT. CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JUDCA J. INORG. CHEM.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	JUPCA J. INORG. SPEC. PAPER	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NATUA NATURE, LOND.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NATUA NATURWISSENSCHAFTEN	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NJHIA NEUES JB. MINER. ABH.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NLNUO NMINERALOG. MAG.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	MRDVA MNR. RES. BULL.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	MURUA MUR. RES. BULL.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NAHUA SOC. AMER. SPEC. PAPER	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NATUA NATURE, LOND.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NATUA NATURWISSENSCHAFTEN	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NJHIA NEUES JB. MINER. ABH.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NLNUO NMINERALOG. MAG.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	MRDVA MNR. RES. BULL.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	MURUA MUR. RES. BULL.	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NAHUA SOC. AMER. SPEC. PAPER	
TI+4 VI			74 CICHA	52 2175 Y3 VS V	NATUA NATURE, LOND.	
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TI+4 VI			74 CICHA	52 2175 Y3 VS V	NATUA NATURE, LOND.	
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compounds to be slightly larger than those of the Eu^{2+} compounds. This difference was assumed to exist for all Sr^{2+} and Eu^{2+} coordinations. Because compounds of Am^{2+} and Sr^{2+} have similar cell volumes, the radius of Am^{2+} was made equal to that of Sr^{2+} .

Wolfe & Newnham (1969) studied $\text{Bi}_{4-x}\text{RE}_x\text{Ti}_3\text{O}_{12}$ and concluded that Bi^{3+} and La^{3+} have nearly equal radii. From a study of BiTaO_4 Sleight & Jones (1975) have concluded that although Bi^{3+} and La^{3+} have essentially equal radii, the size of Bi^{3+} depends on the degree of the $6s^2$ lone-pair character. When BiTaO_4 transforms from a structure where the lone-pair character is dominant to the LaTaO_4 structure, it undergoes a volume reduction. Table 3 shows a comparison of isotropic Bi^{3+} and La^{3+} compounds where the lone-pair character of Bi^{3+} is (1) constrained and (2) dominant. Bi pyrochlores such as $\text{Bi}_2\text{Ru}_2\text{O}_7$, $\text{Bi}_2\text{Ir}_2\text{O}_7$ and $\text{Bi}_2\text{Pt}_2\text{O}_7$ were omitted from the table because no corresponding La pyrochlore exists, but they have unit-cell volumes close to those of the Sm or Nd pyrochlores and thus have smaller volumes than those of La. When Bi^{3+} is forced into high symmetry, a Bi^{3+} compound has a smaller volume than that of La^{3+} , but when the lone-pair character is dominant, the Bi^{3+} compound is distorted and Bi^{3+} and La^{3+} compounds have approximately equal volumes. This behavior was also noted in the highly symmetric garnet structure where the hypothetical $\text{Bi}_3\text{Fe}_5\text{O}_{12}$ was estimated to have cell dimensions between those of the hypothetical $\text{Nd}_3\text{Fe}_5\text{O}_{12}$ and $\text{Pr}_3\text{Fe}_5\text{O}_{12}$ (Geller, Williams, Espinosa, Sherwood & Gilleo, 1963). For practical purposes, Bi^{3+} is listed as slightly smaller than La^{3+} but this dependence on lone-pair character must be kept in mind when comparing the volumes of Bi^{3+} and La^{3+} compounds. Similar behavior may also exist for Pb^{2+} and Sr^{2+} , but this relationship was not investigated.

Table 3. Cell volumes of isotropic Bi^{3+} and La^{3+} compounds

(a) Lone pair character of Bi^{3+} constrained

Compound	Cell volume	Ratio
$\text{BiLi}(\text{MoO}_4)_2$	314.7	0.96
$\text{LaLi}(\text{MoO}_4)_2$	328.7	
$\text{BiNa}(\text{MoO}_4)_2$	320.5	0.97
$\text{LaNa}(\text{MoO}_4)_2$	332.1	
BiOF	87.6	0.90
LaOF	97.7	
BiOCl	110.7	0.95
LaOCl	116.8	
BiOBr	123.8	0.98
LaOBr	126.4	
BiPO_4	293.0	0.96
LaPO_4	304.7	

(b) Lone pair character of Bi^{3+} dominant

Bi_2MoO_6	268.5 ($\times 8$)	1.00
La_2MoO_6	267.3	
BiFeO_3	62.49 ($\times 6$)	1.03
LaFeO_3	60.77 ($\times 4$)	
$\text{Bi}_2\text{Sn}_2\text{O}_7$	1219.9 ($\times 8$)	1.00
$\text{La}_2\text{Sn}_2\text{O}_7$	1225.3	

A similar study of relative cell volumes of isotopic compounds involving the pairs Cu^+-Li^+ , Ag^+-Na^+ , Tl^+-Rb^+ , and $\text{Pb}^{2+}-\text{Sr}^{2+}$ was used to obtain more reliable estimates of the radii of Cu^+ , Ag^+ , Tl^+ , and Pb^{2+} (Shannon & Gumperman, 1975).

The nature of Sn^{2+} , NH_4^+ , and H^- made it impossible to define their ionic radii. The coordination of Sn^{2+} by oxygen or fluorine is always extremely irregular,* leading to average distances which depend on the degree of distortion. Since this distortion varies widely from one compound to another, it is not meaningful to define an ionic radius.

Khan & Baur (1972) derived an apparent radius of the NH_4^+ ion by analyzing the N–O distances in a large number of ammonium salts. They concluded that NH_4^+ has an octahedral radius of 1.61 Å, between that of Rb^+ (1.52 Å) and Cs^+ (1.67 Å). Alternatively, cell volumes of NH_4^+ and Rb^+ fluorides, chlorides, bromides, iodides and oxides may be compared. This leads to the conclusion that NH_4^+ is not significantly different in size from Rb^+ . No explanation is offered for this inconsistency and therefore the radius of NH_4^+ is not included.

The radius of the hydride ion, H^- , has been the subject of some controversy. A number of different radii have been proposed: 2.08 (Pauling, 1960); 1.40 (Gibb, 1962); and 1.53 Å (Morris & Reed, 1965). Gibb studied interatomic distances in many hydrides and concluded that good agreement between observed and calculated distances could be obtained using $r^{(\text{VIH}^-)} = 1.40$ Å if corrected for cation and anion coordination. The value of $r^{(\text{IVH}^-)}$ was taken to be 1.22 Å.

Morris & Reed (1965) concluded that differences in observed distances in hydrides were caused by the large H^- polarizability. Because of such wide variations in the apparent H^- radius, it was omitted. However, an explanation for the variations based on covalence differences will be discussed later.

* Although cell dimensions of $\text{Sn}_2\text{M}_2\text{O}_7$ pyrochlores were used in SP 69 to derive $r^{(\text{VIII}^{\text{III}}\text{Sn}^{2+})}$, Stewart, Knop, Meads & Parker (1973) and Birchall & Sleight (1975) recently found that the pyrochlore A site in $\text{Sn}_2\text{Ta}_2\text{O}_7$ is not fully occupied. Thus, even this example of apparently regular Sn^{2+} polyhedra is not valid.

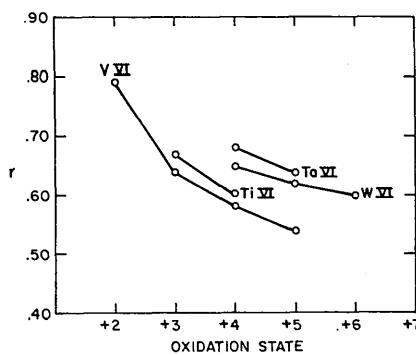
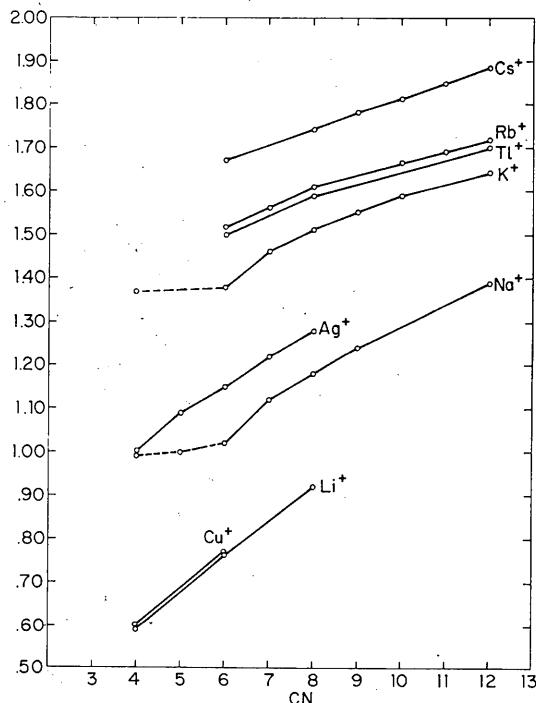


Fig. 1. Effective ionic radius (Å) vs oxidation state.

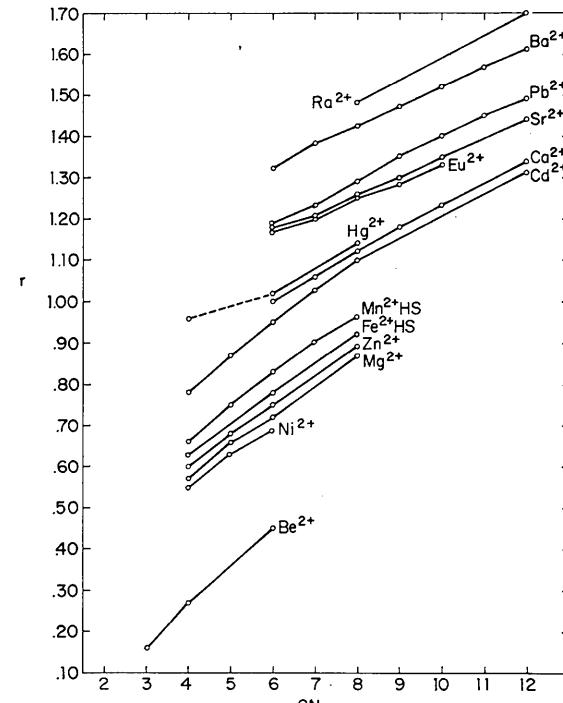
Results and discussion

In Table 1 two sets of radii are included. The first is a set of traditional radii based on $r(\text{VI O}^{2-}) = 1.40 \text{ \AA}$. The

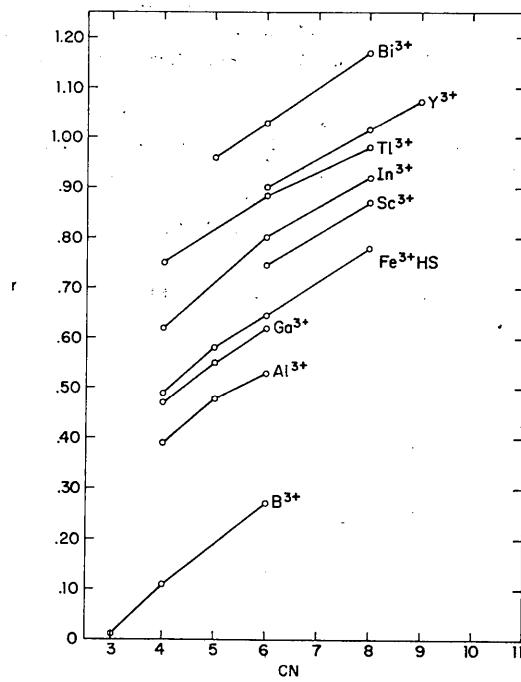
other set is based on $r(\text{VI O}^{2-}) = 1.26$ and $r(\text{VI F}^-) = 1.19 \text{ \AA}$, and corresponds to crystal radii as defined by Fumi & Tosi (1964). As pointed out in SP 69, crystal radii differ from traditional radii only by a constant factor



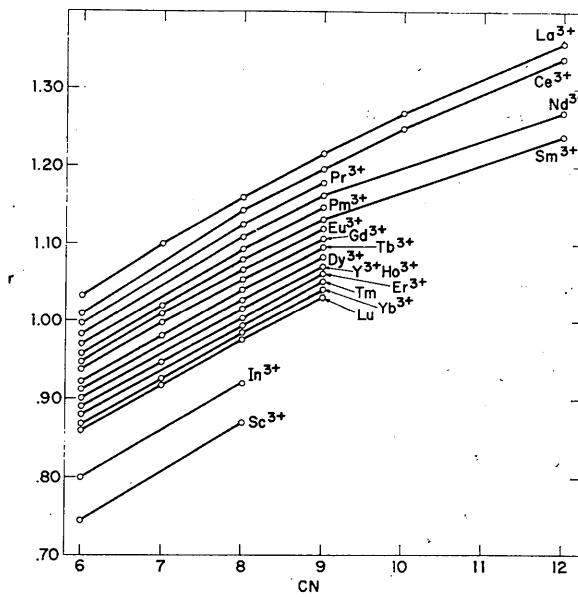
(a)



(b)



(c)



(d)

Fig. 2. (a)–(e) Effective ionic radius (\AA) vs CN for some common cations.

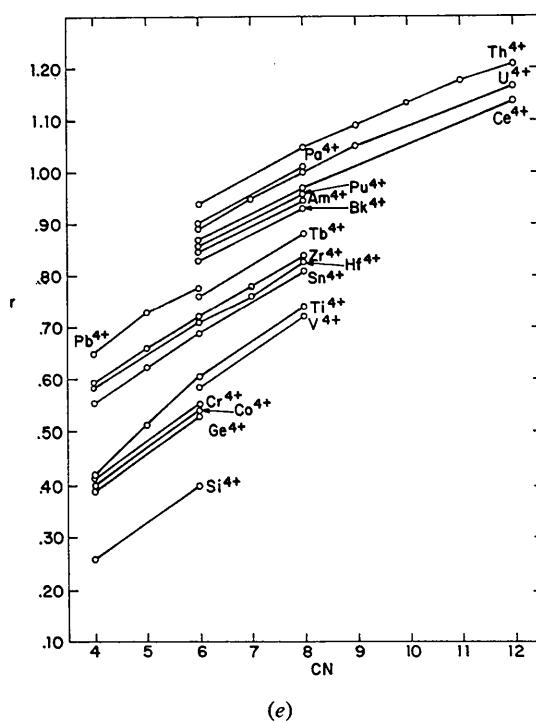


Fig. 2. (cont.)

of 0.14 \AA . Although their inclusion in Table 1 may seem superfluous, it is felt that crystal radii correspond more closely to the physical size of ions in a solid. They should be used, for example, in discussions of closest packing of spheres, structure field maps (Muller & Roy, 1974), and diffusion in solids (Flygare & Huggins, 1973). Traditional radii have been retained because of their familiarity to crystal chemists and physicists. They will probably continue to be used for comparison of unit-cell volumes and interatomic distances. In the table, the ion is followed by electron configuration (EC), coordination number (CN), spin state (SP), crystal radius (CR), and effective ionic radius (IR), and in the last column, a symbol indicating the derivation of the radii and their reliability. Those with a question mark are doubtful because of: uncertainty in CN, or deviation from radii *vs* CN, or radii *vs* valence plots. Where at least five structural determinations resulted in radii differing by no more than $\pm 0.01 \text{ \AA}$, the values are marked with an asterisk.

When the choice of a radius was influenced by any of the various correlations described earlier, it is indicated by the following: *R* – from r^3 *vs* unit cell volume plots; *C* – calculated from bond length–bond strength equations; *E* – estimated from one or more plots of *r* *vs* valence, *r* *vs* CN, and *r* *vs* cell volume. *E* implies poor or nonexistent structural data. Radii in this category include $\text{VI}^{+}\text{Fe}^{2+}\text{LS}$, $\text{VI}^{+}\text{Mn}^{2+}\text{LS}$, $\text{VI}^{+}\text{Cr}^{2+}\text{LS}$, $\text{VI}^{+}\text{V}^{2+}$, $\text{VI}^{+}\text{No}^{2+}$, $\text{VI}^{+}\text{Ni}^{3+}\text{HS}$, $\text{VI}^{+}\text{Ir}^{3+}$, $\text{VI}^{+}\text{Mo}^{3+}$, $\text{VI}^{+}\text{Ta}^{3+}$, $\text{VI}^{+}\text{Pa}^{3+}$, $\text{VI}^{+}\text{Ta}^{4+}$, $\text{IV}^{+}\text{Pb}^{4+}$, $\text{VI}^{+}\text{Ir}^{5+}$, $\text{VI}^{+}\text{Os}^{5+}$, $\text{VI}^{+}\text{Re}^{5+}$, $\text{VI}^{+}\text{Pu}^{5+}$, $\text{VI}^{+}\text{Bi}^{5+}$,

$\text{VI}^{+}\text{Os}^{6+}$, $\text{VI}^{+}\text{Re}^{6+}$, and $\text{VI}^{+}\text{Os}^{7+}$. The symbol *A* means that Ahrens (1952) ionic radius was used whereas *P* means Pauling's (1960) crystal radius was used. The symbol *M* means that the radius was derived from a compound having metallic conductivity. Distances calculated from these radii may be too small for use in compounds having localized electrons. (See discussion *Effects of electron delocalization*.)

In addition, the sources of the radii are indicated in Table 2.

Fig. 2(a)–(e) shows that *r*–CN plots are reasonably regular. Notable exceptions are $\text{IV}^{+}\text{Na}^{+}$, $\text{V}^{+}\text{Na}^{+}$, and $\text{IV}^{+}\text{K}^{+}$. It is apparent that Na–O and K–O distances do not decrease as much as anticipated from the *r*–CN curve* when the CN falls below six. Typical distances and corresponding radii in Table 4 show that Na–O distances in four-coordination are only slightly less than in six-coordination. The reduction in interatomic distances is caused primarily by the decreased repulsive forces due to fewer ligands according to the expression of Pauling (1960):

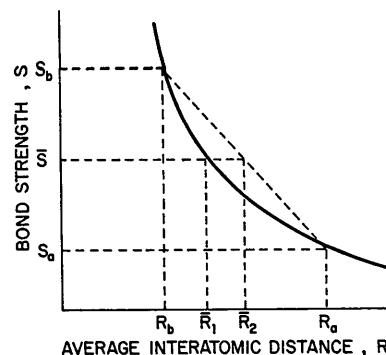
$$\frac{R_{\text{CsCl}}}{R_{\text{NaCl}}} = \left[\frac{A_{\text{NaCl}}}{A_{\text{CsCl}}} \frac{B_{\text{CsCl}}}{B_{\text{NaCl}}} \right]^{1/(n-1)}$$

where *R*=interatomic distance, *A*=Madelung constant, *B*=the cation CN and *n*=Born repulsion coefficient. It appears that this equation is not valid for four-coordinated Na^{+} or K^{+} .

There are a few small irregularities in *r*–CN plots probably caused by poor or insufficient data, *e.g.* curves for Ti^{3+} *vs* Y^{3+} . The differences in slopes of Ti^{4+} *vs* Cr^{4+} and V^{5+} *vs* As^{5+} are probably caused by Ti^{4+} –O and V^{5+} –O octahedra being generally more distorted, which leads to greater average interatomic distances.

It is also interesting to compare distances in square planar coordination *versus* tetrahedral coordination. Radii of square planar Cu^{2+} and Ag^{+} are equal to or slightly greater than corresponding tetrahedral radii, consistent with the trend anticipated from anion

* Extrapolation of the Na curve gives $r(\text{IV}^{+}\text{Na}^{+})=0.90 \text{ \AA}$.

Fig. 3. Typical bond length *vs* bond strength plot.

repulsion effects. A similar comparison with Fe^{2+} and Ni^{2+} cannot be made because of electron distribution changes from tetrahedral to square planar coordination.

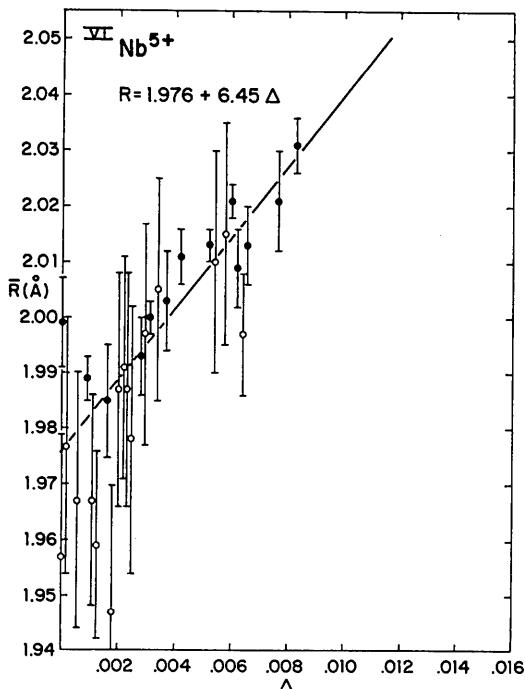


Fig. 4. Mean Nb^{5+} –O bond length vs distortion. Vertical bars represent average e.s.d.'s quoted by the authors. Solid circles represent more accurate data.

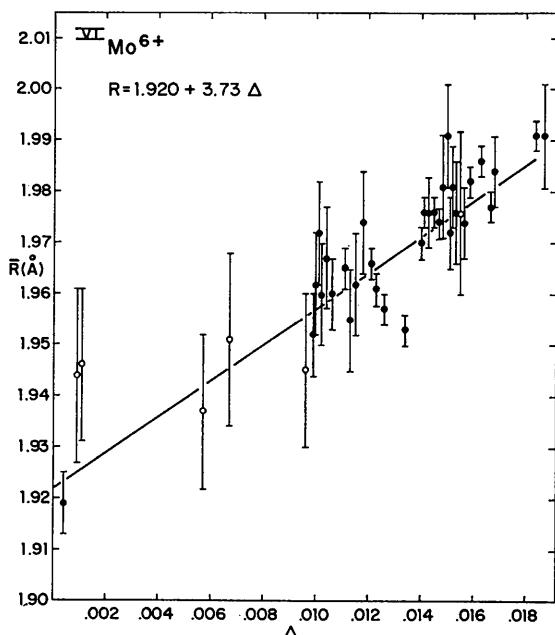


Fig. 5. Mean Mo^{6+} –O bond length vs distortion.

Table 4. Interatomic distances in some compounds containing tetrahedral and octahedral Na^+

Compound	\bar{R} (Å)	r (Å)	Reference
(a) $\text{v}^{\text{I}}\text{Na}^+$			
Na_2O	2.40	1.02	
$\text{Na}_5\text{P}_3\text{O}_{10}$	2.37	0.99	60 ACCRA 13 263
$\text{NaOH}\cdot\text{H}_2\text{O}$	2.36	1.00	57 ACCRA 10 462
Na_6ZnO_4	2.39	0.99	69 ZAACAA409 69
	Mean 2.38	1.00	
(b) $\text{v}^{\text{II}}\text{Na}^+$			
Na_2WO_4	2.38	1.00	74 ACBCA 30 1872
$\text{NaC}_6\text{O}_7\text{H}_7$	2.37	1.01	65 ACCRA 19 561
$\text{Na}_4\text{Sn}_2\text{Ge}_4\text{O}_{12}(\text{OH})_4$	2.39	1.02	70 ACSAA 24 1287
$\text{Na}_2\text{P}_2\text{O}_7\cdot 10\text{H}_2\text{O}$	2.48	1.10	64 ACCRA 17 672
NaHCO_3	2.44	1.06	65 ACCRA 18 818
$\text{Na}_2\text{B}_4\text{O}_6(\text{OH})_2\cdot 3\text{H}_2\text{O}$	2.41	1.04	67 SCIEA 154 1453
$\text{Na}_4\text{P}_4\text{O}_{12}\cdot 4\text{H}_2\text{O}$	2.415	1.05	61 ACCRA 14 555
$\text{NaAl}(\text{SO}_4)_2\cdot 12\text{H}_2\text{O}$	2.45	1.10	67 ACCRA 22 182
$\text{NaB}(\text{OH})_4\cdot 2\text{H}_2\text{O}$	2.460	1.09	63 ACCRA 16 1233
NaU acetate	2.375	1.025	59 ACCRA 12 526
$\text{C}_{10}\text{H}_{12}\text{N}_2\text{NaO}_6\text{P}\cdot 6\text{H}_2\text{O}$	2.406	1.046	75 ACBCA 31 19
	Mean 2.42	1.05	

Factors affecting mean interatomic distances

Additivity of radii to give mean interatomic distances is not so important to the synthetic chemist who is primarily interested in ionic radii for predicting substitution in crystal structures. Crystallographers and physicists, however, are concerned with comparing calculated and experimental interatomic distances and predicting distances, e.g. for distance least-squares (DLS) structure refinements (Baur, 1972; Tillmanns, Gebert & Baur, 1973; Dempsey & Strens, 1975). The effective ionic radii in Table 1 can be used to reproduce moderately well most average interatomic distances in oxides and fluorides. However, certain deviations do occur. Some of these are unexplained but others can be attributed to (1) polyhedral distortion, (2) covalence, (3) partial occupancy of cation sites, or (4) electron delocalization.

1. Polyhedral distortion

To see the effects of polyhedral distortion consider the relationship between bond length (R) and Pauling bond strength (s) (Brown & Shannon, 1973). The analytical expression $s = s_0(R/R_0)^{-N}$, where s_0 is an ideal bond strength associated with R_0 , and R_0 and N are fitted parameters, was evaluated for cation–oxygen pairs for the first three rows of the periodic table. Using these relationships, the sums of bond strengths about cations and anions were found to equal the valences with a mean deviation of about 5 %. Accepting the approximate validity of Pauling's second rule, $p = \sum s$ where p = valence, it is possible to derive the effects of distortion of various polyhedra on their mean bond distances. Fig. 3 shows a typical R - s curve. An undistorted octahedron results in an average bond strength \bar{s} and a mean distance \bar{R}_1 . A distorted octahedron with three bonds of length R_a and three of length R_b results in the same average bond strength, \bar{s} , but a mean distance $\bar{R}_2 > \bar{R}_1$.

The effects of distortion on mean bond lengths in numerous polyhedra have been determined. Although distortions in tetrahedra are not as important as in octahedra, they can contribute to variations in mean tetrahedral distances (Baur, 1974; Hawthorne, 1973). Strongly distorted octahedra like those containing V^{5+} , Cu^{2+} , and Mn^{3+} show a significant variation in mean distance with distortion, Δ^* (Brown & Shannon, 1973; Shannon & Calvo, 1973a; Shannon, Gumerman & Chenavas, 1975). Octahedra containing Mg^{2+} , Zn^{2+} , Co^{2+} , and Li^{+} are generally less distorted than those of V^{5+} , Cu^{2+} , and Mn^{3+} and show a less pronounced dependence on mean bond length (Brown & Shannon, 1973).

The effects of distortion on mean bond lengths in Nb^{5+} -O and Mo^{6+} -O octahedra are illustrated in Figs. 4 and 5. Tables 5 and 6 list the data used to derive the figures.

Table 7 lists the results of linear regression analyses of mean bond length on distortion for all octahedra studied. It is clear from Fig. 4 that undistorted Nb^{5+} octahedra in pyrochlores have a distinctly smaller mean value than in compounds like $NbOPO_4$, $CaNb_2O_6$, and Na_3NbO_4 . Most of the accurately refined molybdates have relatively distorted octahedra. However, certain ordered perovskites with no octahedral distortion such as Ba_2CaMoO_6 would be expected to have much smaller mean Mo^{6+} -O distances than a typical molyb-

date. In fact, the Mo^{6+} -O octahedra in $Mo_2(O_2C_6Cl_4)_6$ with a very small distortion have the short mean distance of 1.919 Å.

Table 7 also lists the results of regression analyses for Ta^{5+} -O and W^{6+} -O octahedra but they are only approximate because of the scarcity of accurate structural data. Analysis of Ti^{4+} -O octahedra was unsuccessful because of scatter in the data. Distances in $Ba_6Ti_{17}O_{40}$ (Tillmanns & Baur, 1970) and $BaTiO_3$ (Evans, 1951) deviated significantly from a linear relation.

Relations between mean distance and distortion should be particularly useful to help determine oxidation states in mixed valence compounds with such combinations as Mo^{5+} - Mo^{6+} , W^{5+} - W^{6+} , V^{4+} - V^{5+} , Nb^{4+} - Nb^{5+} and Mn^{3+} - Mn^{4+} . Such considerations helped rationalize Mn-O distances in $NaMn_7O_{12}$ and the mineral pinakiolite (Shannon, Gumerman & Chenavas, 1975).

The radii in Table 1 are generally derived for an average degree of distortion. Thus, interatomic distances calculated from these radii may be inaccurate if the distortion in a particular compound is much less or greater than usual. This applies particularly to cations whose polyhedra frequently show a large distortion, e.g. Mo^{6+} , Nb^{5+} , V^{5+} , Ba^{2+} , and the alkali ions.

2. Effects of partial occupancy of cation sites on mean cation-anion distances

In compounds with partially occupied sites, abnormally large cation-anion distances are usually found, as expected if the anions surrounding unoc-

* Octahedral distortion is defined by $\Delta = \frac{1}{6} \sum (R_i - \bar{R}/\bar{R})^2$ where \bar{R} =average bond length and R_i =an individual bond length.

Table 5. Comparison of mean octahedral Nb^{5+} -O distances with distortion

Only structures with e.s.d.'s for Nb-O distances of < 0.025 Å were used.

Compound	\bar{R} (Å)	$\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$	Distortion	Reference	
$Hg_2Nb_2O_7$	1.999	0	68 INOCA	7	1704
$Cd_2Nb_2O_7$	1.957	0	72 CJCHA	50	3648
$Na_2Nb_2O_{11}$	1.977	1	70 JSSCB	1	454
$Ba_{0.27}Sr_{0.75}Nb_2O_{5.78}$	1.967	6	61 JCPSA	48	5048
$Na_{13}Nb_{35}O_{94}$	1.965	7	71 JSSCB	3	89
$Ba_3Si_4Nb_6O_{26}$	1.989	9	70 ACBCA	26	102
$Na_{13}Nb_{35}O_{94}$	1.967	11	71 JSSCB	3	89
$Na_{13}Nb_{35}O_{94}$	1.959	12	71 JSSCB	3	89
$Na_{13}Nb_{35}O_{94}$	1.964	12	71 JSSCB	3	89
$NaNbO_3$	1.985	16	69 ACBCA	25	851
$Na_{13}Nb_{35}O_{94}$	1.947	18	71 JSSCB	3	89
$Na_{13}Nb_{35}O_{94}$	1.991	22	71 JSSCB	3	89
$Na_{13}Nb_{35}O_{94}$	1.987	22	71 JSSCB	3	89
$Na_{13}Nb_{35}O_{94}$	1.978	24	71 JSSCB	3	89
$LiNb_2O_8$	1.993	28	71 ACSAA	25	3337
$LiNbO_3$	2.000	31	66 JCPSA	27	997
$Ca_2Nb_2O_7$	1.997	31	74 JINCA	36	1965
$Ca_2Nb_2O_7$	2.005	34	74 JINCA	36	1965
$SbNbO_4$	2.003	37	65 CCJDA	1965	611
$KNbO_3$	2.011	42	67 ACACA	22	639
Na_3NbO_4	2.013	52	74 BUFCA	97	3
$Ca_2Nb_2O_7$	2.010	53	74 JINCA	36	1965
$Ca_2Nb_2O_7$	2.015	58	74 JINCA	36	1965
Na_3NbO_4	2.021	60	74 BUFCA	97	3
$CaNb_2O_6$	2.021	76	70 AMMIA	55	90
$GaNbO_4$	2.031	83	65 ACACA	18	874

Table 6. Comparison of mean octahedral Mo⁶⁺-O distances with distortion
Only structures with e.s.d.'s for Mo-O distances of <0.025 Å were used.

Compound	\bar{R} (Å)	Distortion $\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$	Reference	
Mo ₂ (O ₂ C ₆ Cl ₄) ₆	1.919	5	75 JACSA	97
Mo ₄ O ₁₁ orthorhombic	1.944	9	63 ARKEA	21
Mo ₄ O ₁₁ monoclinic	1.946	10	63 ARKEA	21
Mo ₄ O ₁₁ monoclinic	1.937	56	63 ARKEA	21
Mo ₄ O ₁₁ orthorhombic	1.951	67	63 ARKEA	21
Mo ₄ O ₁₁ orthorhombic	1.911	96	63 ARKEA	21
Mo ₄ O ₁₁ monoclinic	1.945	96	63 ARKEA	21
(C ₁₅ H ₁₁ O ₂) ₂ MoO ₂	1.952	99	74 ACBCA	30
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.962	99	75 JCSIA	1975
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.972	101	75 JCSIA	1975
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.960	104	75 JCSIA	1975
LiMoO ₂ AsO ₄	1.967	104	70 ACSAA	24
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.960	106	74 ACBCA	30
HgMoO ₄	1.965	111	73 ACBCA	29
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.955	113	75 JCSIA	1975
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.962	115	75 JCSIA	1975
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.974	118	68 JACSA	90
MoO ₃ ·2H ₂ O	1.966	121	72 ACBCA	28
MoO ₃ ·2H ₂ O	1.961	123	72 ACBCA	28
MoO ₃ ·2H ₂ O	1.957	126	72 ACBCA	28
MoO ₃ ·2H ₂ O	1.953	134	72 ACBCA	28
(NH ₄) ₅ [MoO ₃) ₅ (PO ₄) (HPO ₄)].3H ₂ O	1.970	140	74 JCSIA	1974
Na ₃ (CrMo ₆ O ₂₄ H ₆).8H ₂ O	1.976	141	70 INOCA	9
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.976	141	74 ACBCA	30
Na ₃ CrMo ₆ O ₂₄ H ₆ .8H ₂ O	1.976	143	70 INOCA	9
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄) (HPO ₄)].3H ₂ O	1.974	145	74 JCSIA	1974
(NH ₄) ₆ [TeMo ₆ O ₂₄].Te(OH) ₆ .7H ₂ O	1.981	147	74 ACBCA	30
CoMoO ₄	1.991	150	65 ACACA	19
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.972	151	74 ACBCA	30
MoO ₃	1.981	151	63 ARKEA	21
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.976	152	68 JACSA	90
K ₂ {[MoO ₂ (C ₂ O ₄)(H ₂ O)] ₂ O}	1.976	152	64 INOCA	3
(NH ₄) ₆ Mo ₈ O ₂₇ ·4H ₂ O	1.974	152	74 ACBCA	30
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄) (HPO ₄)].3H ₂ O	1.982	159	74 JCSIA	1974
Na ₃ CrMo ₆ O ₂₄ H ₆ .8H ₂ O	1.986	163	70 INOCA	9
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄) (HPO ₄)].3H ₂ O	1.977	167	74 JCSIA	1974
MoO ₃ ·H ₂ O	1.984	167	74 ACBCA	30
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄) (HPO ₄)].3H ₂ O	1.991	186	74 JCSIA	1974
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	1.991	189	75 JCSIA	1975
(NH ₄) ₆ [Mo ₇ O ₂₄]·4H ₂ O	2.008	197	75 JCSIA	1975

Table 7. Variation of mean M-O distance and effective ionic radius in octahedral environments as a function of distortion

Ion	Maximum $\Delta \times 10^4$	N^*	R_0 †	r_0 ‡	m	Correlation coefficient	Goodness of fit ($\times 10^3$)
Mo ⁶⁺	212	38	1.920		3.73	0.74	67
				0.572	3.01	0.63	70
W ⁶⁺	122	7	1.925		3.30	0.75	19
				0.565	3.28	0.66	24
V ⁵⁺	576	16	1.887		2.62	0.98	8
Nb ⁵⁺	83	29	1.976		6.45	0.69	71
				0.599	6.83	0.44	99
Ta ⁵⁺	79	6	1.984		6.70	0.81	18
				0.617	3.79	0.15	46
Mn ³⁺	71	15	1.994		7.08	0.82	30
				0.624	6.15	0.54	50
Cu ²⁺	316	26	2.085		3.99	0.82	77
Mg ²⁺	156	28	2.094		8.31	0.72	21
				0.728	8.86	0.77	18
Co ²⁺	46	15	2.106		7.38	0.42	19
				0.734	11.70	0.70	16
Zn ²⁺	71	16	2.099		7.70	0.64	21
				0.736	8.20	0.74	16
Li ⁺	148	11	2.159		8.42	0.81	30
				0.784	9.02	0.79	35

* N = number of independent octahedra

† $R = R_0 + m\Delta$.

‡ $r = r_0 + m\Delta$.

cupied sites relax toward their bonded cation neighbors. Therefore average distances should increase as the occupancy factor decreases. In general, partial occupancy seems to be more prevalent for cations which are weakly bonded to oxygen like Cu^+ , Ag^+ , alkali ions, and large alkaline earths. The most prominent examples are Li and Na compounds. Table 8 summarizes the existent data on some structures with partial cation occupancy. Fig. 6 shows the dependence of mean Li-O bond length on the degree of occupancy. Although the data are not extensive, it is apparent that mean distance increases as occupancy factor decreases. Extrapolation of the Li curve in Fig. 6 to zero occupancy, *i.e.* a tetrahedral Li vacancy, gives 2.10–2.15 Å, which is close to the 2.11 Å found for $\alpha\text{-Li}_5\text{GaO}_4$ by Stewner & Hoppe (1971) and for β eucryptite by Tscherry, Schulz & Laves (1972).

Another example of the effects of partial occupancy can be found in the non-stoichiometric feldspar $\text{Sr}_{0.84}\text{Na}_{0.03}\square_{0.13}\text{Al}_{1.69}\text{Si}_{2.29}\text{O}_8$ reported by Grundy & Ito (1974). The mean Sr-O distance in this compound is 0.03 Å greater than in the stoichiometric $\text{SrAl}_2\text{Si}_2\text{O}_8$ (Chiari, Calleri, Bruno & Ribbe, 1975).

The relation between mean distance and occupancy probably cannot be quantified precisely because the relaxation of oxygen ions will depend on the nature and number of other cation neighbors.

3. Effects of covalence

Changes in interatomic distances due to covalence effects are anticipated in compounds with (1) anions less electronegative than fluorine or oxygen, *i.e.* chlorine, bromides, sulfides, selenides, *etc.* and (2) tetrahedral oxyanions such as the VO_4^{3-} and AsO_4^{3-} groups. The effects of covalence show up as a lack of additivity of the radii and are generally referred to as 'covalent shortening'.

(a) *Halides and chalcogenides*. Covalence effects can be observed by comparing the relative contraction of cation-anion distances in two different isotropic compounds as the anion becomes less electronegative, *e.g.* Fe^{2+} in Fe_2GeO_4 and Fe_2GeS_4 vs Mg^{2+} in Mg_2GeO_4 and Mg_2GeS_4 . Covalence shortens both Fe-S and Mg-S bonds relative to Fe-O and Mg-O bonds, but because of the greater electronegativity of Fe^{2+} (1.8) compared to Mg^{2+} (1.2), the Fe-S bonds are shortened to a greater extent. Thus a 'covalency contraction' parameter (Shannon & Vincent, 1974) can be defined:

$$R_d = \frac{d(\text{Fe}-\text{X})^3}{d(\text{Mg}-\text{X})^3}$$

where $d(\text{Fe}-\text{X})$ = mean Fe-X distance.

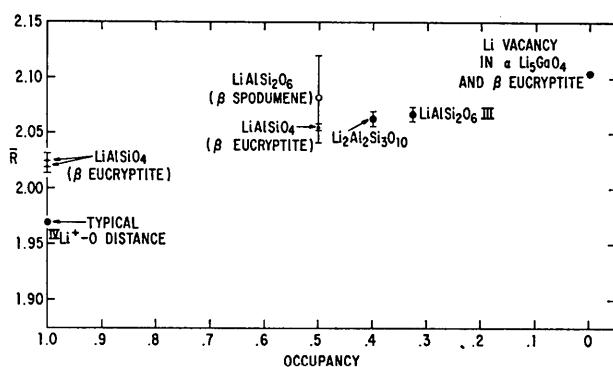
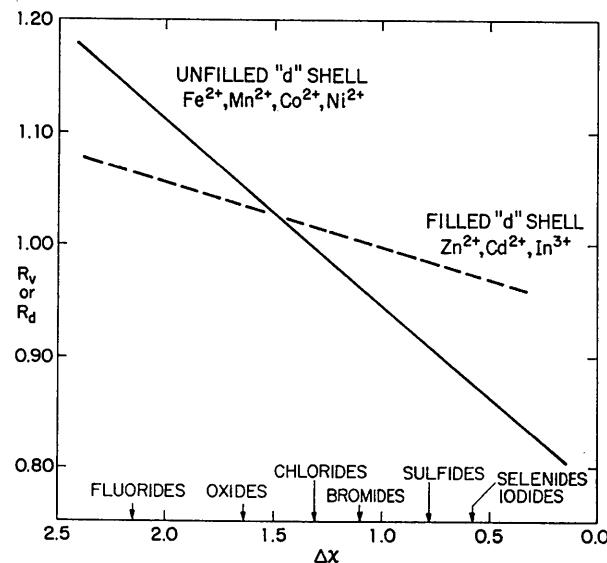
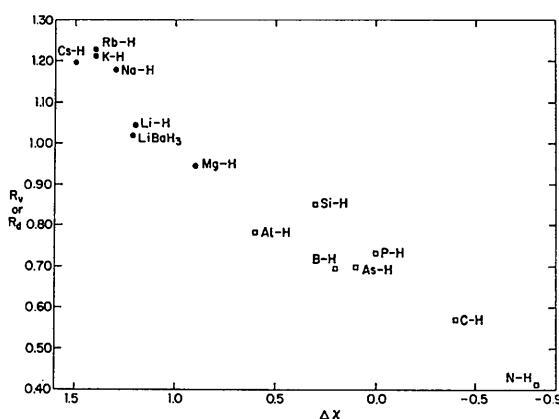
A similar parameter

$$R_v = \frac{V(\text{Fe}_m\text{X}_n)}{V(\text{Mg}_m\text{X}_n)}$$

compares the volume of an Fe^{2+} compound with that of an isotropic Mg^{2+} compound. To see the effects of covalence on the Fe-X distance relative to the Mg-X distance, the ratio R_v or R_d may be plotted against the difference in electronegativity of the Fe-X bond, $\Delta\chi_{\text{Fe}-\text{X}}$. Such schematic R_v - $\Delta\chi$ plots are shown in Fig. 7. The reference ions for Cd^{2+} and In^{3+} are Ca^{2+} and Sc^{3+} respectively. Such plots usually show a strong

Table 8. Mean distances in structures with partially occupied cation sites

Compound	Occupancy factor	\bar{R}	Reference			
<i>(a) IVLi^+</i>						
Typical LiAlSiO_4 (β eucryptite)	1.00	1.97	Table 1			
	1.00	2.020 (4)	73 AMMIA	58	681	
		2.025 (7)	72 ZKKKA	135	175	
$\text{LiAlSi}_2\text{O}_6$ II (β spodumene)	0.50	2.08 (4)	68 ZKKKA	126	46	
		2.085 (9)	69 ZKKKA	130	420	
LiAlSiO_4 (β eucryptite)	0.50	2.056 (2)	72 ZKKKA	135	161	
$\text{Li}_2\text{Al}_2\text{Si}_3\text{O}_{10}$	0.40	2.064 (4)	70 ZKKKA	132	118	
$\text{LiAlSi}_2\text{O}_6$ III	0.33	2.068 (5)	68 ZKKKA	127	327	
$\alpha\text{-Li}_5\text{GaO}_4$	0.00	2.11	71 ACBCA	27	616	
LiAlSiO_4	0.00	2.11	72 ZKKKA	135	175	
<i>(b) VINa^+</i>						
Typical $\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wyllieite)	1.00	2.42	Table 1			
	0.91	2.533 (6)	74 AMMIA	59	280	
NaSbO_3	0.82	2.74	74 JSSCB	9	345	
$\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wyllieite)	0.70	2.723 (6)	74 AMMIA	59	280	
$\text{NaAlSi}_2\text{O}_8$ (high albite)	0.50	2.600 (9)	69 ACBCA	25	1503	
$\text{NaAl}_{11}\text{O}_{17}$ ($\beta\text{-Al}_2\text{O}_3$)	0.35	2.839 (1)	68 ZKKKA	127	94	
NaSbO_3	0.29	2.65	74 JSSCB	9	345	
$\text{Na}_{2.58}\text{Al}_{21.81}\text{O}_{34}$ ($\beta\text{-Al}_2\text{O}_3$)	0.25	2.88	71 ACBCA	27	1826	
<i>(c) VIAg^+</i>						
Typical AgSbO_3	1.00	2.50	Table 1			
	0.44	2.64	74 JSSCB	9	345	
AgSbO_3	0.33	2.75	74 JSSCB	9	345	
$\text{Ag}_{2.4}\text{Al}_{22}\text{O}_{34.2}$	0.22	2.83	72 JSSCB	4	60	

Fig. 6. Mean $\text{Li}^+–\text{O}$ bond length vs partial occupancy.Fig. 7. Covalency contraction parameter, R_v or R_d , vs $\Delta\chi$ for filled and unfilled *d* shell cations.Fig. 8. Covalency contraction parameter, R_v or R_d , vs $\Delta\chi$ for hydrides. Solid circles represent ratios of cell volumes of isotypic compounds. Squares represent ratios of the cubed $\text{M}-\text{H}$ distances to the cubed $\text{M}-\text{F}$ distances.

dependence of R_v on $\Delta\chi$. For $\text{Fe}^{2+}-\text{Mg}^{2+}$ the Fe^{2+} fluoride volumes are $\sim 110\%$ of the corresponding Mg^{2+} fluoride volumes whereas the Fe^{2+} sulfide volumes are $\sim 96\%$ of the corresponding Mg^{2+} sulfide volumes. Plots for the cations with filled 'd' shells show a markedly smaller dependence on $\Delta\chi$. This appears to be due to the difference in covalence of hybrid orbitals formed from metal 'd' orbitals *vs* metal 's-p' orbitals.

These relations show that effective ionic radii derived primarily from oxides are not strictly applicable to fluorides – note the change in R_v for $\text{Fe}^{2+}, \text{Co}^{2+}, \text{Ni}^{2+}$, and Mn^{2+} from fluorides to oxides. This effect is particularly noticeable in $R_v-\Delta\chi$ plots for the pairs Cu^+-Li^+ and Ag^+-Na^+ (Shannon & Gumerman, 1975). The Cu^+-Li^+ and Ag^+-Na^+ plots are very steep, *e.g.* the volume of AgF is 120% of the volume of NaF , whereas the volume of Ag_2Se is only 72% of the volume of Na_2Se . Although most of this change arises from covalency, double repulsion effects present in the Li and Na halides described by Pauling (1960) may also play a role.

Covalence effects are useful in explaining certain differences between the effective ionic radii of Table 1 and the ionic radii of Pauling (1927) and Ahrens (1952). Pauling's radii for Cu^+ (0.96 Å) and Ag^+ (1.26 Å) are considerably larger than those in Table 1 (0.77 and 1.15 Å respectively). Since these radii were derived from comparison of alkali halide distances, using an equation relating effective nuclear charge and screening constants (Pauling, 1927), they are valid in primarily ionic crystals. The smaller radii in Table 1 are applicable in the more covalent oxides. Extrapolation of R vs $\Delta\chi$ curves such as in Fig. 7 leads to values of 0.91 Å and 1.23 Å for fluorides, which are close to Pauling's ionic values.

A final example of covalence effects concerns M^+-H^- distances. According to Gibb (1962), the radius of the hydride ion is slightly larger than the radius of the fluoride ion. To rationalize the behavior of the hydride ion, the $\text{M}-\text{H}$ bond has been treated as covalent. Therefore, it is useful to make R_v vs $\Delta\chi$ plots similar to those just discussed for $\text{Fe}^{2+}, \text{Cu}^+$, etc. In this case, the reference ion is F^- and volumes of certain hydrides are compared to those of isotypic fluorides. The results of this analysis are shown in Fig. 8. The solid circles represent volume ratios, $R_v = V(\text{M}_m\text{H}_n)/V(\text{M}_m\text{F}_n)$; open squares represent ratios of typical distances $R_d = d(\text{M}-\text{H})^3/d(\text{M}-\text{F})^3$. In the more ionic hydrides of Cs, Rb, K, and Na, hydride volumes are considerably larger than those of the fluorides. For the Li and Mg compounds, hydride and fluoride volumes are approximately equal, whereas the more covalent hydrides have increasingly smaller relative volumes than the corresponding fluorides. Fig. 8 partly explains the differences in reported radii. The Morris & Reed (1965) value of 1.53 Å was derived essentially from the large alkali halides, while Gibb's value of 1.40 Å was derived primarily from hydrides of the more electronegative

metals such as: Sc, Ti, Y, Zr, Hf, Nb, Ta, and Th. Because of this strong dependence of M–H distances on cation electronegativity, it does not seem very useful to quote a unique radius for H^- .

(b) *Tetrahedral oxyanions.* Lack of additivity also appears in most small tetrahedral groups and is particularly noticeable for the ions $V^{IV}B^{3+}$, $V^{IV}Fe^{3+}$, $V^{IV}Ge^{4+}$, $V^{IV}As^{5+}$, $V^{IV}V^{5+}$, $V^{IV}S^{6+}$, $V^{IV}Se^{6+}$, and $V^{IV}Cl^{7+}$. The deviations in vanadates have been studied in detail (Shannon & Calvo, 1973b). Assuming that the V–O bond is strongly covalent, and that relatively electronegative cations such as Cu^{2+} , Ni^{2+} , and Co^{2+} tend to remove electron density from the V–O bond, a V–O bond length increase in Cu, Ni, and Co vanadates is anticipated. Plots of mean radii (\bar{r}) vs mean cation electronegativity ($\bar{\chi}$) show a marked slope with a gradual increase in $\bar{r}(V^{IV}V^{5+})$ from vanadates of the alkali and alkaline earth ions to those of Cu, Ni, and Co. Similar plots for other ions, P^{5+} , As^{5+} (Shannon & Calvo, 1973b), B^{3+} , Si^{4+} , Se^{6+} (Shannon, 1975), showed the same behavior. The statistical data on the tetrahedra of B^{3+} , Si^{4+} , Ge^{4+} , P^{5+} , As^{5+} , S^{6+} , Se^{6+} , Cr^{6+} , Mo^{6+} , W^{6+} , and Cl^{7+} have been summarized by Shannon (1975). The slopes of the \bar{r} vs $\bar{\chi}$ plots were greatest for V^{5+} , Se^{6+} , and Cl^{7+} , and least for Si^{4+} . Although the evidence for covalence as the origin of these effects in the above systems is only indirect, this behavior is consistent with accepted ideas of ‘covalent shortening’ of bonds.

The evidence for covalent shortening of $V^{IV}Fe^{3+}$ –O bonds is more direct. Jeitschko, Sleight, McClellan & Weiher (1976) have found a good correlation between (1) the Fe Mössbauer isomer shift and mean Fe–O distance and (2) $\bar{\chi}$ and mean Fe–O distance (\bar{R}). Thus, in β -Na FeO_2 $\bar{R}=1.86$ Å and $\delta=0.18$ mm s $^{-1}$ relative to α Fe whereas in Bi $_3$ (FeO $_4$) (MoO $_4$) $_2$ $\bar{R}=1.909$ Å and $\delta=0.282$ mm s $^{-1}$.

4. Effects of electron delocalization

At a pressure of 6.5 kbar SmS (NaCl structure) undergoes a semiconductor to metal transition and a reduction in cell edge from 5.97 to 5.70 Å (Jayaraman, Narayananmurti, Bucher & Maines, 1970). The reduction in cell volume was attributed to a partial conversion of Sm $^{2+}$ to Sm $^{3+}$; some of the electrons presumably go into a conduction band.

Electron delocalization effects can also be seen by comparing the volumes of the conducting V sulfides VS, V_7S_8 , V_3S_4 and V_5S_8 with the corresponding Cr sulfides which have localized ‘d’ electrons (de Vries & Jellinek, 1974). The V compounds have volumes $\sim 5\%$ smaller than the corresponding chromium compounds. This does not agree with the relative sizes of V and Cr in oxides and fluorides, e.g. $r(V^{IV}V^{3+})=0.64$ and $r(V^{IV}Cr^{3+})=0.615$ Å. For the sulfides, this unit-cell volume anomaly is not simply attributable to metallic vs semiconducting behavior. While Cr_3S_4 , Cr_5S_6 , and Cr_7S_8 show a positive temperature dependence of resistivity typical of a metal, magnetic susceptibility

measurements indicate Curie–Weiss behavior and therefore nearly localized electrons (van Bruggen, 1969). This is in contrast to the Pauli paramagnetic behavior of the corresponding V sulfides (de Vries & Haas, 1973) characteristic of delocalized electrons. Thus, in SmS and the sulfides of V metallic character accompanied by electron delocalization appears to be associated with reduced bond distances.

A further example of delocalization effects occurs in the compound NaVS $_2$ (Weigers, van der Meer, van Heinigen, Kloosterboer & Alberink, 1974). The molecular volume of Pauli paramagnetic NaVS $_2$ I (67.9 Å 3) is significantly less than that of NaVS $_2$ II (72.7 Å 3). NaVS $_2$ II is characterized by localized electrons (Jellinek, 1975) and its molecular volume is consistent with that of isotypic NaCrS $_2$ (71.1 Å 3).

If electron delocalization in oxides results in reduced metal–oxygen distances and thereby an effective increase in valence, radii derived for the ions Mo $^{4+}$, Tc $^{4+}$, Ru $^{4+}$, Rh $^{4+}$, W $^{4+}$, Re $^{4+}$, Os $^{4+}$, and Ir $^{5+}$ from metallic oxides may not be reliable when applied to insulating oxides. Thus, radii obtained from distances in the metallic phases, e.g. RhO $_2$, ReO $_2$, and Cd $_2$ Ir $_2$ O $_7$, will be smaller than radii obtained from semiconducting or insulating compounds.* When both types of compounds have been studied, a significant difference in distances is generally found. The mean octahedral Re $^{4+}$ –O distance in insulating K $_4$ [Re $_2$ O $_2$ (C $_2$ O $_4$) $_4$]·3H $_2$ O (Lis, 1975) of 2.021 (10) Å ($r=0.671$ Å) is greater than the estimated mean distance in metallic ReO $_2$ of 1.99 Å ($r=0.63$ Å). Knop & Carlow’s (1974) value of $r=0.662$ Å derived from cell volumes of the insulating Cs $_2$ ReF $_6$ phases is consistent with the radius of Re $^{4+}$ from K $_4$ [Re $_2$ O $_2$ (C $_2$ O $_4$) $_4$]·3H $_2$ O. The Re $^{5+}$ –O distance in Nd $_4$ Re $_2$ O $_{11}$ (Wilhelmi, Lagervall & Muller, 1970) of 1.987 (12) Å ($r=0.607$ Å) is significantly greater than the distance in metallic Cd $_2$ Re $_2$ O $_7$ (Sleight, 1975) of 1.93 (2) Å ($r=0.55$ Å). The radii of 0.58 Å derived from XeF $_5$ RuF $_6$ and 0.60 Å from XeFRuF $_6$ (Bartlett, Gennis, Gibler, Morrell & Zalkin, 1973) are greater than the radius of 0.565 Å derived from the r^3 – V plot for metallic Cd $_2$ Ru $_2$ O $_7$. In contrast, however, the Mo $^{4+}$ radius of 0.64 Å derived from insulating Li $_2$ MoF $_6$ (Brunton, 1971) is not greatly different from the radius of 0.65 Å derived from metallic MoO $_2$ (Brandt & Skapski, 1967).

Although there appears to be ample evidence to show that M–O bond distances in compounds with localized electrons are greater than M–O distances in compounds with delocalized electrons, the data are not yet sufficient to derive a reliable set of radii for semiconducting compounds containing Mo $^{4+}$, Tc $^{4+}$, Ru $^{4+}$, Rh $^{4+}$, W $^{4+}$, Re $^{4+}$, Os $^{4+}$, and Ir $^{5+}$. This will become possible as additional accurate structure refinements of fluorides, molecular inorganic compounds, and semiconducting oxides containing these ions become available.

* This assumes that metallic character can be equated with delocalized electron behavior in these compounds.

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